#### 2017 NCSD Topical Meeting

Sept 10-15, 2017 Carlsbad, NM

Tutorials Sept 10, 2017

## Monte Carlo Criticality Calculations with MCNP6-Whisper

#### LA-UR-17-27058



• Los Alamos NATIONAL LABORATORY EST. 1943 Forrest Brown, Jennifer Alwin, Michael Rising

Monte Carlo Methods, Codes, & Applications (XCP-3) X Computational Physics Division

## Abstract

#### Monte Carlo Criticality Calculations with MCNP6-Whisper

#### Forrest Brown, Jennifer Alwin, Michael Rising Monte Carlo Methods, Codes, & Applications, LANL

#### **Review of MC criticality fundamentals (9am - 11am)**

• This portion of the tutorial session is targeted at new or early-career criticality safety analysts to provide a review of basic concepts, including: best practices for MC criticality calculations, spectra, lethargy, sensitivity, nuclear data uncertainties, etc.

#### What's new with MCNP6.2 & Whisper-1.1 (11am - 12pm)

• An update on what is the same or different with the 2017 release of MCNP6.2 & Whisper-1.1.

#### **Tutorial on using MCNP6-Whisper-1.1 for NCS validation (1pm - 5pm)**

- Whisper-1.1 makes use of MCNP6-generated sensitivity profiles and cross-section covariance data to provide guidance for setting baseline USLs for NCS validation. Background & practical application of the new tool will be covered, along with discussion of ANS standards.
- Discussion time will be available for specific issues concerning installation, problem resolution, user issues, computational details, etc.
- Laptops are not required, but participants with laptops & installed MCNP6 can follow the demonstrations hands-on.

Acknowledgment: This work was supported by the US DOE-NNSA Nuclear Criticality Safety Program.

#### **Schedule & Lecture Material**

#### **MORNING:**

Introduction

**Neutron Physics & Statistical Methods** 

- a) Neutron Spectra
- b) Nuclear Data Sensitivities
- c) Covariance Data For Nuclear Cross-sections
- d) Correlation Coefficients

**Best Practices For Monte Carlo Criticality Calculations** 

What's new with MCNP6.2 & Whisper-1.1

#### **AFTERNOON:**

Validation For Nuclear Criticality Safety Application To Nuclear Criticality Safety Validation

a) Introduction

- b) Benchmark Selection Ck's
- c) Extreme Value Theory Bias, Bias Uncertainty
- d) MOS For Nuclear Data Uncertainty GLLS
- **Practical Use Of Sensitivity-Uncertainty Tools** 
  - b) Introduction Scale-Tsunami & Mcnp6-Whisper
  - c) MCNP/Whisper Whisper\_mcnp, Whisper\_usl

#### Examples

- a) Pu Pyrochemical Processing -
- b) HEU examples
- c) General Studies

Using Whisper to Support NCS Validation ANS-8.24 Requirements

#### Lecture notes from:

LA-UR-17-27058, Brown, Rising, Alwin Sensitivity-Uncertainty Techniques for Nuclear Criticality Safety

#### Additional notes from:

LA-UR-17-24260, Brown, Rising, Alwin Release of MCNP6.2 & Whisper-1.1 -Guidance for NCS Users

LA-UR-17-24406, Brown, Rising, Alwin Verification of MCNP6.2 for Nuclear Criticality Safety Applications

LA-UR-17-25009, Brown, Investigation of Clustering in MCNP6 Monte Carlo Criticality Calculations

# Sensitivity-Uncertainty Techniques for Nuclear Criticality Safety

LA-UR-17-27058



• Los Alamos NATIONAL LABORATORY EST. 1943 Forrest Brown, Michael Rising, Jennifer Alwin

Monte Carlo Methods, Codes, & Applications (XCP-3) X Computational Physics Division

### Abstract

#### **Sensitivity-Uncertainty Techniques for Nuclear Criticality Safety**

#### Forrest Brown, Michael Rising, Jennifer Alwin Monte Carlo Codes Group, LANL

The sensitivity and uncertainty analysis course will introduce students to  $k_{eff}$  sensitivity data, cross-section uncertainty data, how  $k_{eff}$  sensitivity data and  $k_{eff}$  uncertainty data are generated and how they can be used. Discussion will include how sensitivity/uncertainty data can be used to select applicable critical experiments, to quantify a defensible margin to cover validation gaps and weaknesses, and in development of upper subcritical limits.

Acknowledgment: This work was supported by the US DOE-NNSA Nuclear Criticality Safety Program.

## Outline

#### **Sensitivity-Uncertainty Techniques for Nuclear Criticality Safety**

- 1. Introduction
- 2. Validation For Nuclear Criticality Safety
- 3. Neutron Physics & Statistical Methods
  - a) Neutron Spectra
  - b) Nuclear Data Sensitivities
  - c) Covariance Data For Nuclear Cross-sections
  - d) Correlation Coefficients

#### 4. Application To Nuclear Criticality Safety Validation

- a) Introduction
- b) Benchmark Selection C<sub>k</sub>'s
- c) Extreme Value Theory Bias, Bias Uncertainty
- d) MOS For Nuclear Data Uncertainty GLLS

#### 5. Practical Use Of Sensitivity-Uncertainty Tools

- a) Review: Best Practices For Monte Carlo Criticality Calculations, also LA-UR-17-25009 – Clustering in MC Criticality Calculations
- b) Introduction Scale/Tsunami & Mcnp6/Whisper
- c) MCNP/Whisper Whisper\_mcnp, Whisper\_usl

#### 6. Examples

- a) Pu Pyrochemical Processing Geometry, Materials, Reflection, Moderation
- b) HEU examples
- c) General Studies
- 7. Using Whisper to Support NCS Validation ANSI/ANS-8.24 Requirements
- 8. References

#### Introduction – NCS Validation

#### **Big Picture:**

- Calculations used to support nuclear criticality safety evaluations must make use of validated computer codes
- Computer code validation:
  - Compare calculated results to nature (ie, experimental measurements)
  - Must compare to experiments similar to application of interest
  - Determine how accurate the codes are
- Conservatism is fundamental to NCS
  - Always consider uncertainties in calculations, data, measurements
  - Use additional margin for uncertainties that cannot be calculated
  - Subtract uncertainties from upper subcritical limits on K<sub>eff</sub>
- Codes are great, but analyst judgment is required for everything

## Introduction – NCS validation

#### **Upper Subcritical Limit (USL)**

- For an application:
  - A calculated  $K_{eff}$  < 1.0 is NOT sufficient to ensure subcriticality
  - Must conservatively account for
    - Bias & uncertainties in the calculational method
    - Uncertainties in the physical model (eg, mass, isotopics, geometry, ...)



#### Introduction – NCS validation

- Nuclear Criticality Safety requires validation of computational methods
- Validation involves comparing calculation vs experiment for many benchmarks similar to the application of interest
- Neutron spectra are complex functions of geometry, materials, nuclear data, etc.
- The figure shows neutron production spectra for 5 Pu systems:
  - an application (Case 28)
  - 4 benchmarks for Pu systems
- Which of the benchmarks are similar to the application?



Energy (MeV)

During the past 20 years, powerful tools have been developed based on sensitivityuncertainty methods

1e-9

1e-7

1e-5

- From ORNL, the Scale system includes Keno, Tsunami, Tsurfer, & other tools
- From LANL, the MCNP6 & Whisper tools are now available
- Other tools have been developed by groups in England, France, Germany, Japan, S. Korea, China

#### $v\Sigma_F \Phi$ production spectrum

#### LA-UR-17-27058 7

#### **Introduction - Sensitivity Profiles for Nuclear Data**

• The sensitivity coefficient is the ratio of relative change in k-effective to relative change in a system parameter:

$$S_{k,x} = \frac{dk/k}{dx/x} = -\frac{\left\langle \psi^{\dagger}, \left(\Sigma_{x} - S_{x} - k^{-1}F_{x}\right)\psi\right\rangle}{\left\langle \psi^{\dagger}, k^{-1}F\psi\right\rangle}$$

- $S_{k,x}(E)$  is the sensitivity profile, that includes all isotopes, reactions, & energies for a system:
- MCNP6 & Scale/Tsunami Monte Carlo can use the Iterated Fission Probability method to compute adjoint-weighted integrals for the sensitivity profiles
  - Tally scores are collected in original generation, adjoint-weighting is based on the progeny in the asymptotic generation



#### Introduction - Sensitivity-Uncertainty Methodology for NCS



## Introduction – Goals

- Review of Validation for NCS
  - Overview, requirements, standards, definitions, USL
  - Selecting benchmarks, bias & bias uncertainty, validation approaches
- Fundamental Concepts for Sensitivity-Uncertainty Methods
  - Spectra
  - Sensitivity of  $K_{eff}$  to nuclear data
  - Covariances for the nuclear data
  - Correlation coefficients & the sandwich rule
- Application to NCS Validation
  - Computing correlation coefficients & selecting benchmarks
  - Determining bias & bias uncertainty
  - Determining (minimum) extra margin for data & other uncertainties
- Practical Examples

# Nuclear Criticality Safety Validation



Introduction - background, standards, definitions, USL, calculational margin, margin of subcriticality Selection of benchmarks Bias & bias uncertainty Sensitivity-uncertainty analysis Validation approaches & technical review



## Background

- Why do we care about Validation?
  - ANSI/ANS-8.24 Foreword: "...the industry need to optimize operations and reduce unnecessary conservatism has increased. Thus, the scrutiny and importance placed on validation has increased in recent years."
  - Ensure what NCS determines to be subcritical is actually subcritical
    - Computer codes have approximations and errors
    - Nuclear data have approximations and errors
  - Criticality safety:
    - Focus on avoiding worst-case combination of mistakes, uncertainties, errors
    - Rigor & conservatism always; never wishful thinking or "close enough"
  - How can we be confident in assessing subcriticality?
    - Verify that codes work as intended
    - Validate codes + data + methods against nature (experiments)

## Orders, Standards, Guides for NCS

- 10 CFR 830 Subpart A, Quality Assurance
- 10 CFR 830 Subpart B, Nuclear Safety Management
- DOE O 414.1C, Quality Assurance
- DOE G 414.1-4, Safety Software Guide for use with 10CFR 830 Subpart A, Quality Assurance Requirements
- DOE G 421.1-2, Implementation Guide for Use in Developing Documented Safety Analyses to Meet Subpart B of 10 CFR 830
- DOE O 420.1C, Facility Safety
- DOE O 426.2 Personnel Selection, Training, Qualification, and Certification Requirements
- DOE-STD-3007-2007, Guidelines for Preparing Criticality Safety Evaluations at DOE Nonreactor Nuclear Facilities
- DOE STD 1134-1999 Review Guide for Criticality Safety Evaluations
- DOE-STD-1158-2010, Self-Assessment Standard for DOE Contractor Criticality Safety Programs
- DOE-STD-3009-1994, Preparation Guide for U.S. Department of Energy Nonreactor Nuclear Facility Safety Analysis
- DOE-STD-1186-2004, Specific Administrative Controls
- DOE-STD-1027-1992, Hazard Categorization and Accident Analysis Techniques for Compliance with DOE Order 5480.23, Nuclear Safety Analysis Reports
- ANSI/ANS-8.1-2014, Nuclear Criticality Safety in Operations with Fissionable Materials Outside Reactors

- ANSI/ANS-8.3-2003, Criticality Accident Alarm System
- ANSI/ANS-8.5-1996(R2007), Use of Borosilcate-Glass Raschig Rings as a Neutron Absorber in Solutions of Fissile Material
- ANSI/ANS 8.7-1998(R2012), Nuclear Criticality Safety in the Storage of Fissile Materials
- ANSI/ANS-8.10-2005, Criteria for Nuclear Criticality Safety Controls in Operations with Shielding and Confinement
- ANSI/ANS 8.14-2004, Use of Soluble Neutron Absorbers in Nuclear Facilities Outside Reactors
- ANSI/ANS 8.17-2004, Criticality Safety Criteria for the Handling, Storage, and Transportation of LWR Fuel Outside Reactors
- ANSI/ANS-8.19-2014, Administrative Practices for Nuclear Criticality Safety
- ANSI/ANS 8.20-1991(R2005), Nuclear Criticality Safety Training
- ANSI/ANS-8.21-1995(R2001), Use of Fixed Neutron Absorbers in Nuclear Facilities Outside Reactors
- ANSI/ANS-8.23-2007, Nuclear Criticality Accident Emergency Planning and Response

#### ANSI/ANS 8.24-2007, Validation of Neutron Transport Methods for Nuclear Criticality Safety Calculations

- ANSI/ANS 8.26-2007, Criticality Safety Engineer Training and Qualification Program
- Validation with Limited Benchmark Data, Response to CSSG Tasking 2014-02

## Background

#### **Establishing Subcriticality**

 Any method used to determine the subcritical state of a fissionable material system must be validated.

#### - Direct use of experimental data is preferred (ANSI/ANS-8.1-2014 4.2.7)

- Where applicable data are available, subcritical limits shall be established on bases derived from experiments, with adequate allowance for uncertainties in the data.
- In the absence of directly applicable experimental measurements, the limits may be derived from calculations made by a method shown by comparison with experimental data to be valid in accordance with Sec. 4.3

#### - (ANSI/ANS-8.1-2014 4.3)

- Validation shall be performed by comparison to experiments and AoA should be established from this comparison.
  - Code-to-code comparison doesn't meet requirement.
- Use of subcritical limit data provided in ANSI/ANS standards or accepted reference publications does not require further validation.

#### Validation: Definitions (1)

- From ANSI/ANS-8.24-2007, Validation of Neutron Transport Methods for Nuclear Criticality Safety Calculations:
  - Verification: The process of confirming that the *computer code* system correctly performs numerical calculations.
  - Validation: The process of quantifying (e.g., establishing the appropriate *bias* and *bias uncertainty*) the suitability of the computer code system for use in nuclear criticality safety analyses.
  - Computer code system: A calculational method, computer hardware, and computer software (including the operating system).
  - Calculational Method: The mathematical procedures, equations, approximations, assumptions, and associated numerical parameters (e.g., cross sections) that yield the calculated results.

## Validation: Definitions (2)

- From ANSI/ANS-8.24-2007, Validation of Neutron Transport Methods for Nuclear Criticality Safety Calculations:
  - Bias: The systematic difference between calculated results and experimental data. [k<sub>eff calculated</sub> k<sub>eff experiment</sub>]
  - Bias Uncertainty: The uncertainty that accounts for the combined effects of uncertainties in the benchmarks, the calculational models of the benchmarks, and the calculational method.
  - Calculational Margin: An allowance for bias and bias uncertainty plus considerations of uncertainties related to interpolation, extrapolation, and trending.
  - Margin of Subcriticality: An allowance beyond the calculational margin to ensure subcriticality.
  - Benchmark Applicability: The benchmark parameters and their bounding values from which bias and bias uncertainty of a calculational method are established. [AoA]
  - Validation Applicability: A domain, which could be beyond the bounds of the benchmark applicability, within which the margins derived from validation of the calculational method have been applied. [extension of AoA]

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#### LA-UR-17-27058 17

## **MCNP Verification & Validation Suites**

#### **Verification Suites**

#### REGRESSION

- 161 code test problems
- Run by developers for QA checking (100s of times per day)

#### • VERIFICATION\_KEFF

- 75 analytic benchmarks (0-D and 1-D)
- Exact solutions for k<sub>eff</sub>
- Past multigroup, New continuous-energy
- Tests basic tracking and power iteration scheme
- VERIFICATION\_GENTIME
  - 10 benchmarks (analytic or comparisons to Partisn) for reactor kinetics parameters

#### KOBAYASHI

- 6 void & duct streaming problems, with point detectors, exact solutions
- Ganapol Benchmarks

**Gonzales Benchmark** 

#### [in progress]

- Exact, semi-analytic benchmark problems
- Fixed source, not criticality

#### [in progress]

 Exact analytic benchmark with elastic scatter, including free-gas scatter

#### **Validation Suites**

#### VALIDATION\_CRITICALITY

- 31 ICSBEP Cases
- Too small a suite for serious V&V
- Today, used for
  - Code-to-code verification, with real problems & data
  - Compiler-to-compiler verification, with real problems & data
  - Timing tests for optimizing MCNP coding & threading

#### VALIDATION\_CRIT\_EXPANDED

- 119 ICSBEP Cases
- Broad-range validation, for developers

#### VALIDATION\_CRIT\_WHISPER

- 1101 ICSBEP Cases
- Used with Whisper methodology for serious validation
- Will be expanded, as time permits

## **Overview of Validation Methods**

- Identify the range of applications to be considered
  - Fissile material, geometry, reflection, moderation, etc.
  - Metrics to help characterize neutronics EALF, % fast/thermal fissions, H/U or H/Pu for solutions, etc.
- Select a set of experimental benchmarks from ICSBEP Handbook that are neutronically similar to the applications
  - Must select sufficient number for valid statistical analysis
  - Analyze the set of benchmarks with Monte Carlo
- Statistical analysis
  - Determine bias & bias uncertainty for the set of benchmarks
  - For conservatism, usually set positive overall bias to zero & only consider negative bias for the benchmark collection
- Estimate additional margin of subcriticality (MOS)
  - Extra margin to account for nuclear data uncertainty
  - Extra margin to account for unknown code errors
  - Extra margin if applications not similar enough to benchmark set

## **Upper Subcritical Limit**

 To consider a simulated system subcritical, the computed k<sub>eff</sub> must be less than the Upper Subcritical Limit (USL):

 $K_{calc} + 2\sigma < USL$ 

## USL = 1 + (Bias) - (Bias uncertainty) - MOS

#### [additional AoA margin may be appropriate]

Note: Bias = calculated – experiment,

For conservatism – can set positive biases to zero; only consider negative biases

- The bias and bias uncertainty are at some confidence level, typically 95% or 99%.
  - These confidence intervals may be derived from a normal distribution, but the normality of the bias data must be justified.
  - Alternatively, the confidence intervals can be set using nonparametric methods.

## **Calculational Margin**

- The calculational margin is the sum of the bias and the bias uncertainty.
  - Bias: represents the systematic difference between calculation and benchmark experiments.
  - Bias uncertainty: relates to uncertainties in the experimental benchmarks and the calculations.
  - Bias & bias uncertainty are routine calculations, for a given application & set of benchmarks
  - Bias & bias uncertainty are only credible when the application & chosen benchmarks are neutronically similar
  - Often quoted as 95/95 confidence, meaning that the calculation margin bounds 95% of the benchmark deviations at the 95% confidence level (assuming normality).

## **Calculational Margin Example**

- Hypothetical bias curve
  - Selected experiments with Pu metal and water mixtures



## Margin of Subcriticality

- To establish a Margin of Subcriticality (MOS) need to consider the process, validation, codes, data, etc. holistically.
  - Confidence in the codes and data.
    - More mature codes that are widely used have greater confidence than newer ones.
    - Deterministic methods may require additional margin beyond Monte Carlo because of numerical issues (e.g., ray effects, discretization errors, self-shielding approximations, etc.).

#### Adequacy of the validation

- Unlikely to find a benchmark experiment that is exactly like the model being simulated.
- Based on trending analysis of physical parameters and/or sensitivity and uncertainty studies, can quantify "similarity".
- Sparsity of benchmark data, extrapolations, and wide interpolations necessitate larger margins.

## Major contributors

- Margin for uncertainties in nuclear cross-section data
- Margin for unknown errors in codes
- Additional margin to consider the limitations of describing process conditions based upon sensitivity studies, operating experience, administrative limits, etc.

- Select critical experiments that you expect to have the same bias as the criticality safety evaluation models
  - Similar neutron energy spectrum (EALF, ANECF, etc.)
  - Similar fissionable materials and isotopics
  - Similar neutron absorbers (Cd, Gd, B, Fe, Ti, etc.)
  - Similar neutron reflectors (water, steel, lead, concrete, etc.)
  - Similar geometries
- Due to variation in criticality safety evaluation models, you may need multiple sets or sets covering a parameter range
  - Especially when considering upset conditions

#### • How many experiments are needed?

- As many experiments that are similar or "applicable" to the criticality safety evaluation models for valid statistical analysis
- If an experiment is exactly the same as the fissionable material operation, subcritical limits may be derived directly from experiments with no need to calculate the result
- "Response to CSSG Tasking 2014-02, Validation with Limited Benchmark Data," September 21, 2015, http://ncsp.llnl.gov/cssg/taskandresponse/2014/2014-02\_Response\_on\_Validation\_with\_Limited\_Data\_09-21-15.pdf
- If no benchmark experiments exist that match the system being evaluated, it may be possible to interpolate or extrapolate from existing benchmark data to that system. Sensitivity and uncertainty analysis tools may be used to assess the applicability of benchmark problems to the system being analyzed. (DOE-STD-3007-2007)

- Historically, engineering judgement ("expert") has been used
  - Based on the analysts understanding of what is important to the problem

#### • This can lead to questions

- Validation of U solution with U metal experiments
- Experiments with strong absorbers included that were not present in safety models
- Validation of fuel rod lattices with solution or metal experiments
- Overly broad critical experiment set (i.e., single broad validation set) used.

The validation applicability should not be so large that a subset of the data with a high degree of similarity to the system or process would produce an upper subcritical limit that is lower than that determined for the entire set. This criterion is recommended to ensure that a subset of data that is closely related to the system or process is not nonconservatively masked by benchmarks that do not match the system as well (ANSI/ANS-8.24 7.2)



## Engineering judgement

- Could take years of experience and study of individual benchmarks
- Could rely on guidance from other qualified analysts to caution (missing materials, neutron absorbers present in typical materials not always obvious, etc.)

#### ANSI/ANS-8.24 Section 5

- Identify the parameters that correlate experiments to the system or process being analyzed in the criticality safety evaluation
- Normal and credible abnormal conditions shall be considered when determining the parameters and range of parameters
  - The experiments selected need to be similar to the normal and abnormal conditions you need to evaluate
- Experiments shall be reviewed for completeness and accuracy before being used in a validation
  - An experiment may be useful for setting limits, but not be sufficiently complete or accurate to use as a benchmark (This can happen with subcritical experiments, process specific experiments, and in-situ experiments)
- Benchmarks should cover the parameter range
  - Avoid the need to extrapolate beyond the range of the available data
- Benchmarks selected should be consistent with the modeling capabilities of the code system being validated

#### ANSI/ANS-8.24 Section 5

- Benchmarks should be drawn from multiple sources to minimize systemic error
- Methods used to analyze benchmarks shall be the same computational method being used in the criticality safety evaluation
  - Albedos, variance reduction techniques, cross section processing, sometimes geometry options
- Benchmark modeling shall be the responsibility of individuals
  experienced in the use of the *computational method*
- Benchmark models prepared by outside organizations should be evaluated for appropriateness, completeness & accuracy
  - ICSBEP handbook cautions against using their input files without review
  - Modeling techniques used may not be adequately similar to that used in the criticality safety evaluation models

## **Calculating Bias and Bias Uncertainty**

- There are many methods and codes used to calculate bias and bias uncertainty. Some examples are:
  - NUREG/CR-6698 (Methods originally developed at SRNL)
  - USLSTATS
  - Whisper
- The validation study should describe (i.e., either directly or by reference) the method used to calculate the bias and bias uncertainty.
- Make sure the data meets all prerequisites (e.g., normality, number of points, etc.) for the method used. If not, use a different method.
- In general, positive biases\* (calculated value is higher than experiment value) are not credited for criticality safety purposes. If they are used, shall be justified based on an understanding of the cause of bias. (Positive biases are sometimes used in reactor or nuclear experiment design.)

\*The sign of the bias is arbitrary. For the purposes of ANSI/ANS-8.24, it has been defined to be positive when the calculated values exceed the experimental values, but it could be defined otherwise.

## **Results Distribution**

- Some bias and bias uncertainty determination methods require that the distribution be "normal"
- Some examples of normality tests
  - Visual inspection of frequency bar charts (qualitative chi-square)
  - Chi-squared tests
  - Kolomogrov-Smirnov
  - Shapiro-Wilk
  - Anderson-Darling
- For trending analysis, look at normality of residuals (difference between best fit line and k<sub>eff,normalized</sub>
- Most normality tests (e.g., those used in USLSTATS and NUREG/CR-6698) accept the distribution as normal unless 95% sure that it is not normal.
- You should do numerical tests for normality, but a histogram plot is sometimes adequate. Look out for distributions with multiple peaks, skewed distributions, and tails that are obviously inconsistent with normal distribution
- Even if you do use numerical tests for normality, you should still do the histogram, and verify to yourself that the pictures and the numbers match.

## S/U Analysis

 Sensitivity analysis quantifies how variation of material properties or nuclear data affects k<sub>eff</sub>.

#### • Techniques:

#### Manual model variation

- Change material densities or temperatures
- Change dimensions
- Used to justify simplifications and to quantify the impact of manufacturing tolerances and uncertainties
- Used to support margin adopted for validation weaknesses

#### - Perturbation theory methods (Whisper and TSUNAMI)

- These systems use perturbation theory to provide nuclide, reaction, energy, and location dependent sensitivity data
- Typically in units of  $(\Delta k/k)/(\Delta \sigma/\sigma)$ , or the fractional change in  $k_{eff}$  due to a fractional change in the nuclear data value.
- Sensitivity analysis improves understanding of what is important for  $\mathbf{k}_{\text{eff}}$  determination

## S/U Analysis

- Uncertainty analysis combines sensitivity data with nuclear data uncertainty information to yield:
  - Uncertainty in k<sub>eff</sub> due to uncertainty in nuclear data for specific nuclides and reactions
  - These uncertainties can be used to provide a defensible basis for margin to cover validation weaknesses
  - The uncertainty information for two different systems may be compared to quantify how much uncertainty the systems have in common
  - If two systems are similarly sensitive to the same nuclear data, then they should have the same bias
  - The  $c_k$  correlation coefficient compares two systems, assessing the potential for common bias for each nuclide, reaction, and energy group
  - C<sub>k</sub> = 1 means two systems use same data in same way

## S/U Analysis

#### • S/U analysis:

- Data can be used to
  - · Select benchmarks that are similar to the application
  - Improve understanding of systems
  - Suggest or defend modeling simplifications
  - Suggest critical experiments that might be useful for validation
  - Critical experiment design
  - In GLLS for estimating margin for data uncertainties (Whisper and TSURFER)
  - Improve understanding of potential bias causes
  - Estimate how large biases related to a mixture or nuclide might be and provide a defensible basis for margin selection to cover validation weaknesses
  - As a trending parameter in USL determination

 CSSG Response on Validation with Limited Data: "For those situations where a nuclide is determined to be important and limited data exist, validation may still be possible. However, an additional margin should be used to compensate for the limited data. This margin is separate from, and in addition to, any margin needed for extending the benchmark applicability to the validation. Sensitivity and uncertainty tools may be used as part of the technical basis for determining the magnitude of the margin."

### **Comparison of Validation Approaches (Simplified)**

	Traditional, Simple	Traditional, Enhanced	Sensitivity-Uncertainty Based
Benchmark Collection	Expert judgment, 1 set to cover all applications	Expert judgment, Several subsets (metal, solutions, other)	Large collection with sensitivity profile data, Reject outliers, Estimate missing uncertainties
Selecting Benchmarks		Expert judgment, Select subset based on geometry & materials	Automatically select benchmarks with sensitivity profiles closest to application
Calculational Margin	Determine bias & bias uncertainty	Determine bias & bias uncertainty, Possible trending within subset	Determine bias & bias uncertainty, Automatically use weighting based on application-specific Ck values
Margin of Subcriticality	Expert judgment, Very large	Expert judgment, Large	Automatically determine specific margin for data uncertainty by GLLS, Code-expert judgment for code, Expert judgment for additional MOS
Comment	Easy to use, Highly dependent on expert judgment, Requires large conservative MOS	More work if trending, Very dependent on expert judgment, Subsets & trending may permit smaller MOS	Computer-intensive, quantitative, Less reliance on expert judgment, Calculated estimate for most of MOS
#### LA-UR-17-27058 33

#### **Documentation and Independent Technical Review**

#### Documentation:

- Sufficient detail to allow for independent technical review
- Describe computer code system being validated
- Justify selection of benchmarks
  - Identify data sources through references
  - Document benchmark applicability (AoA)
- Methods and calculations supporting the determination of bias and bias uncertainty, calculational margin, validation applicability
  - If using trending analysis, document technical bases
- Validation applicability (extension beyond AoA)
  - Justification for extrapolations or wide interpolations
  - Discuss and justify differences between validation applicability and system or process parameters
  - Describe limitations (e.g., gaps in data, missing data)

#### Independent Technical Review:

- review benchmark applicability
- Input files and output files
- Methodology for determining bias, bias uncertainty, margins
- Concurrence with validation applicability

# **Neutron Spectra**

- Neutron slowing down theory
- Lethargy
- Neutron spectra
- Resonance absorption
- Spectral indicators
- Examples

#### **Neutron Slowing Down Theory**

- Consider the transport equation for:
  - Infinite medium of hydrogen
  - Steady source at energy E<sub>S</sub>
  - Isotropic elastic scatter
  - Scattering nuclides are stationary, no upscattering occurs
  - No absorption

$$\Omega \cdot \nabla \phi(E) + \Sigma_T(E)\phi(E) = \int_E^{E_S} dE' \Sigma_S(E' \to E)\phi(E') + S \cdot \delta(E - E_S)$$

- For hydrogen at rest (E >> kT)  $\Sigma_{S}(E' \rightarrow E) = \frac{\Sigma_{S}(E')}{E'}$
- Slowing down in hydrogen at rest:

$$\Sigma_{S}(E)\phi(E) = \int_{E}^{E_{S}} dE' \frac{\Sigma_{S}(E')}{E'} \phi(E') + S \cdot \delta(E - E_{S})$$

• Solution  $\phi(E) = \frac{S}{\Sigma_{S}(E) \cdot E} + \frac{S}{\Sigma_{S}(E)} \delta(E - E_{S})$ 

#### **Slowing Down Theory - Lethargy**

 For theory, visualization, understanding, it is useful to change variables from energy (E) to lethargy (u)

$$u = \ln \frac{E_0}{E}, \text{ where } E_0 \text{ is large, eg 20 MeV}$$
$$du = -\frac{dE}{E}, \quad E = E_0 e^{-u}$$
$$\phi(u) = \left| \frac{dE}{du} \right| \phi(E) = E \cdot \phi(E)$$

- As energy decreases, lethargy increases
- Consider slowing down flux in hydrogen, E<E<sub>s</sub>

$$\phi(E) = \frac{S}{\Sigma_{S}(E) \cdot E} \sim \frac{1}{E}$$
$$\phi(u) = \frac{S}{\Sigma_{S}(u)} \sim \text{constant}$$

**Unit Cell** 

#### Flux Spectra for Neutron Slowing Down & Criticality

hydrogen

hydrogen



water

water + B<sup>10</sup>

water + U<sup>238</sup>

#### Flux Spectra for Neutron Slowing Down



# UO<sub>2</sub> Fuel Pin



## **Characterizing the Neutron Spectrum**

- The neutron spectrum *Φ*(E) or *Φ*(u) is a complex function of geometry, materials, isotopes, reflectors, temperature, cross-sections, ...
- Many different spectral index parameters can be used to characterize the spectrum
  - EALF energy corresponding to the average lethargy of neutrons causing fission
  - ANECF average energy of neutrons causing fission
  - Above thermal leakage fraction
  - H/Pu <sup>239</sup> or H/U<sup>235</sup> ratios, for solutions
  - % fissions caused by fast, intermediate, thermal neutrons
  - (U238 fission)/(U235 fission), and other ratios
  - etc.
- These parameters are useful for comparing different reactors or benchmark experiments, in looking for trends in code or cross-section accuracy
- Spectrum hardness is often characterized by one of these parameters
- No single parameter tells the whole story

## **EALF vs ANECF**

**ANECF** = average neutron energy causing fission

#### EALF = energy of the average neutron lethargy causing fission



#### Pu Systems – v $\Sigma_{\Phi}\Phi$ production & spectrum hardness



# Nuclear Data Sensitivities

#### **Perturbation Theory**

- First-order estimate of the change in some response to a change in some parameter
- In the literature for some time,
  - J. D. LEWINS, *Importance: The Adjoint Function*, Permagon Press, Oxford, United Kingdom (1965).
  - G. I. BELL and S. GLASSTONE, *Nuclear Reactor Theory*, Van Norstrand Reinhold, New York, New York (1970).
- Example: change in reactivity can be estimated,

$$\Delta \rho = -\frac{\left\langle \psi^{\dagger}, \left( \Delta \Sigma_{t} - \Delta S - \frac{1}{k} F \right) \psi \right\rangle}{\left\langle \psi^{\dagger}, F' \psi \right\rangle}$$

• Requires adjoint functions to compute correctly.

## **Adjoint Transport Equation**

• The adjoint transport equation:

$$-\mathbf{\Omega} \cdot \nabla \psi^{\dagger}(\mathbf{r}, \mathbf{\Omega}, E) + \Sigma_{t} \psi^{\dagger}(\mathbf{r}, \mathbf{\Omega}, E) =$$

$$\iint dE' d\mathbf{\Omega}' \Sigma_{s}(\mathbf{r}, \mathbf{\Omega}' \cdot \mathbf{\Omega}, E \to E') \psi^{\dagger}(\mathbf{r}, \mathbf{\Omega}', E')$$

$$+ \frac{1}{k_{\text{eff}}} \iint dE' d\mathbf{\Omega}' \chi(E \to E') v \Sigma_{f}(\mathbf{r}, E) \psi^{\dagger}(\mathbf{r}, \mathbf{\Omega}', E')$$

Adjoint fundamental mode has physical meaning:

The importance at a location in phase space is proportional to the expected value of a measurement, caused by a neutron introduced into a critical system at that location, after infinitely many fission generations.

- MCNP6 uses this basic concept the iterated fission probability to estimate importances for adjoint-weighted tallies
- Note: Neutron balance is enforced in the k-eigenvalue problem regardless of true criticality.

## **Monte Carlo Adjoint Calculations**

- The adjoint transport equation looks very similar to the forward transport equation
- Think of following particles backwards from detector (k<sub>eff</sub>) to source...
  - Requires inverting the scattering laws
    - Complicated for continuous-energy physics
    - Possible for multigroup physics
- Until recently, estimating quantities requiring the adjoint function in continuous-energy Monte Carlo codes was not possible
- The iterated fission probability method is based on estimating the adjoint or importance weighting for continuous-energy Monte Carlo tallies during a normal forward calculation

## **MCNP** Implementation

- MCNP breaks active cycles into consecutive *blocks*:
  - Tally scores are collected in original generation, & progenitor neutrons tagged
  - All subsequent progeny within the latent generations remember their progenitor
  - Importance is the population of progeny from each progenitor in the asymptotic generation
  - (Score)\*(importance) is tallied for adjoint-weighted results



## **Example – Need for Adjoint-Weighting**

MCNP can compute lifetimes (prompt removal times) with non-importance weighted tallies:

unweighted

adjoint-weighted





 Example: Importance weighting is necessary in systems with thick reflectors. Unweighted lifetimes are often very much larger than effective lifetimes (adjoint-weighted)

Neutrons spending significant time deep in the reflector are unlikely to cause fission and are therefore unimportant

Example: Flattop  $\lambda_{\text{No-wgt}} = 67.1 \text{ ns}$  $\lambda_{\text{Adj-wgt}} = 17.5 \text{ ns}$ 



Important neutrons are often short-lived

<u>Net Effect:</u> Not weighting by importance overvalues long-lived neutrons leading to lifetimes much too long.

# Motivation (1)

- Nuclear cross sections are a major driver for criticality, and their uncertainties usually the largest source of bias in calculations.
- Knowing which data most impacts criticality is useful for:
  - Critical experiment design
  - Uncertainty quantification and bias assessment
  - Code validation
  - Nuclear data adjustment and qualification
- Validation requires selecting benchmarks that are appropriate for the process being analyzed.
  - One method of picking appropriate benchmarks is to find the ones where the system multiplication is impacted by the same nuclear data.
  - For example, if the process  $k_{eff}$  is very sensitive to thermal plutonium capture, you should find benchmarks where the same is true.
- Critical experiment design
  - Often experiments are performed to address some defined nuclear data need.
  - Nuclear data sensitivities can determine if the as-designed experiment meets that need.

#### **Sensitivity Coefficient**

- For criticality problems, often want to know:
  - How sensitive is Keff to uncertainty in some parameter ?
- The sensitivity coefficient is defined as the ratio of relative change in a response to a relative change in a system parameter:

$$S_{R,x} = \frac{\Delta R / R}{\Delta x / x}$$

- Here, the response is the system multiplication k and the parameter x is some nuclear data (cross section).
- For a very small change in system parameter x:

$$S_{k,x} = \frac{x}{k} \frac{dk}{dx}$$

## **Sensitivity Coefficient**

• This may be expressed using perturbation theory:

$$S_{k,x} = \frac{x}{k} \frac{dk}{dx} = -\frac{\left\langle \psi^{\dagger}, \left( \Sigma_{x} - \mathbf{S}_{x} - k^{-1} \mathbf{F}_{x} \right) \psi \right\rangle}{\left\langle \psi^{\dagger}, k^{-1} \mathbf{F} \psi \right\rangle}$$

- This includes both the forward and adjoint neutron fluxes.
- The boldface S and F are shorthand for scattering and fission integrals of the transport equation.
- The x subscript implies that the quantity is just for data x.

## **Example 1 – Need for Sensitivities**

- Usage of sensitivity coefficients:
  - How much does Keff change if prompt nubar,  $\bar{v}_{prompt}$ , were perturbed?
    - Could manually perturb prompt nubar to get Keff change, or...
- Linearly expand Keff as a function of prompt nubar:

$$k(\overline{\nu}') \approx k(\overline{\nu}) + \frac{\partial k}{\partial \overline{\nu}} (\overline{\nu}' - \overline{\nu})$$

• Rearranging with:

$$\Delta k = k(\overline{\nu}') - k(\overline{\nu}), \qquad \Delta \overline{\nu} = \overline{\nu}' - \overline{\nu}$$

The sensitivity coefficient appears:

$$\frac{\Delta k}{k} \approx \frac{\overline{v}}{k} \frac{\partial k}{\partial \overline{v}} \cdot \frac{\Delta \overline{v}}{\overline{v}} = S_{k,\overline{v}} \frac{\Delta \overline{v}}{\overline{v}}$$

 Multiplying the <u>sensitivity coefficient</u> by a <u>relative change</u> in prompt nubar results in the first-order estimate of the <u>relative change</u> in Keff.

#### **Example 1 – Need for Sensitivities**

- How much does Keff change with a perturbed <sup>235</sup>U prompt nubar?
  - Godiva problem:



#### **Example 1 – Need for Sensitivities**

#### Conclusions:

#### Adjoint-weighted sensitivity coefficient

- Single calculation
- Very accurate

#### Direct perturbations

- Multiple calculations
- Need to either
  - Edit ACE file
  - Edit ENDF file, run NJOY
- Small perturbations can lead to inaccurate results due to Monte Carlo noise
  - Must grind down statistics



## **Example 2 – Need for Sensitivities**

- Usage of sensitivity coefficients:
  - How uncertain is Keff with respect to the uncertainty in prompt nubar,
    - ?  $\bar{v}_{prompt}$ 
      - Could randomly sample from prompt nubar to see Keff distribution, or...
- Look at moments (mean & variance) of linearly expanded Keff

- Mean: 
$$\mu_{k(\overline{v}')} = k(\overline{v}) + \frac{\partial k}{\partial \overline{v}} (\mu_{\overline{v}'} - \overline{v})$$

$$\sigma_{k(\overline{v}')}^{2} = \left(\frac{\partial k}{\partial \overline{v}}\right)^{2} \sigma_{\overline{v}'}^{2}$$

The sensitivity coefficient appears:

$$\frac{\sigma_{k(\bar{v}')}^2}{k^2} = \left(\frac{\bar{v}}{k}\frac{\partial k}{\partial \bar{v}}\right)^2 \frac{\sigma_{\bar{v}'}^2}{\bar{v}^2} = S_{k,\bar{v}}^2 \frac{\sigma_{\bar{v}'}^2}{\bar{v}^2}$$

 First-order estimate of <u>Keff relative uncertainty</u> due to <u>relative uncertainty</u> in prompt nubar

## **Example 2 – Need for Sensitivities**

- How much uncertainty in Keff is due to uncertainty in <sup>235</sup>U prompt nubar?
  - Godiva problem:



## **Example 2 – Need for Sensitivities**

Conclusions:

#### Adjoint-weighted sensitivity coefficient

- Single calculation
- Very accurate

#### Random sampling

- Multiple calculations
- Need to either
  - Edit ACE file
  - Edit ENDF file, run NJOY
- Many calculations may be needed to fully sample distribution
  - With N=100 prompt nubar realizations

$$\frac{\sigma_{k(\overline{v}')}}{\overline{k}} = \frac{1}{\overline{k}} \sqrt{\frac{1}{N} \sum_{i=1}^{N} \left(k_i - \overline{k}\right)^2} = 0.585\%$$

$$\frac{\sigma_{k(\bar{v}')}}{k} = \sqrt{S_{k,\bar{v}}^2 \frac{\sigma_{\bar{v}'}^2}{\bar{v}^2}} = 0.568\%$$



#### **Examples of Sensitivity Coefficient Profiles**





#### Pu-239: fission chi(E) sensitivity



#### H-1: elastic scattering cross-section sensitivity

**OECD/NEA UACSA Benchmark Phase III.1** 



#### **Cu-63**:

#### **Elastic Scattering Sensitivity**

**Copper-Reflected Zeus experiment:** 



## **MCNP6 - KOPTS Card**

- KOPTS controls many special features for KCODE calculations
- For keff sensitivity calculations, KOPTS is used to control the following:
  - Size of the blocks (default is 10 cycles)
  - Sensitivity output printing (default is just to the output file).
- Format:

## KOPTS BLOCKSIZE= N KSENTAL= FILEOPT

• For now, the only "FILEOPT" allowed is MCTAL, which has MCNP produce a special MCTAL results file

#### MCNP6 - KSEN Card

- Format for nuclear data: KSENj XS ISO= ZAID1 ZAID2 ... RXN= MT1 MT2 ... ERG= E1 E2 ...
- Notes:
  - *j* is an arbitrary user index (> 0).
  - XS defines the type of sensitivity (XS only allowed for now).
  - ISO is followed by a list of ZAIDS or S(a,b) identifiers (e.g., 92235.70c, default is all isotopes).
  - RXN is a list of MT numbers (default is total, see next slide for a shortened list).
  - **ERG** is a user-defined energy grid in MeV (default 0 to infinity).
  - More options available for secondary distributions (e.g., chi).
  - Multiple instances of KSEN are allowed, so long as they have a different user index *j*.

#### **MCNP6 - KSEN Reaction MT numbers**

#### • Partial list of valid reaction MTs for KSEN

– Total	1		
<ul> <li>Capture</li> </ul>	-2		
<ul> <li>Elastic Scattering</li> </ul>	2		
<ul> <li>Inelastic Scattering</li> </ul>	4		
– Fission	-6	or 18	
– Fission Nu	-7	or 452	
– N, 2N	16		
<ul> <li>N, Gamma</li> </ul>	102		
– N, p	103		
– N, d	104		Red = used for Whisper
– N, t	105		
– N, <sup>3</sup> He	106		
<ul> <li>N, alpha</li> </ul>	107		
– Fission Chi	-1018		
<ul> <li>Elastic Law</li> </ul>	-1002		

#### **MCNP6 - KSEN Examples**

- Capture cross section sensitivity for all isotopes
  - ksen1 xs rxn= -2
- U-238 elastic and inelastic scattering sensitivities

ksen2 xs iso= 92238.70c rxn= 2 4

- H-1 and light-water S(a,b) total sensitivity with uniform lethargy grid from 1e-5 eV to 100 MeV
  - ksen3 xs iso= 1001.70c lwtr.10t rxn= 1 erg= 1.e-11 12ilog 1e+2

#### MCNP6 Exercise 1: KSEN Card

- Copy puc6.txt from SOLUTIONS directory to ksen1.txt.
- Find sensitivities to 3 x 2 array of cans containing plutonium nitrate solution.
  - Set KCODE card to use 5000 neutrons per cycle, skip 50, and run 250 cycles total.
  - Set KOPTS card to have a BLOCKSIZE of 5.
  - Add a cross section sensitivity card with no arguments, i.e., use all defaults

kcode 5000 1.0 50 250
...
c
c
### keff sensitivity cards
c
kopts blocksize = 5
c
c default ksen, get total xs sensitivity to all isotopes
c
ksen1 xs

• Run the problem and analyze output.

#### **MCNP6 Exercise 1: Results**

#### nuclear data keff sensitivity coefficients

sensitivity profile	1	
energy range:	0.0000E+00	1.0000E+36 MeV

isotope	reaction	sensitivity	rel. unc.
1001.70c	total	4.7564E-01	0.0589
701 <b>4</b> .70c	total	-1.0670E-02	0.5088
8016.70c	total	1.2197E-01	0.1225
24050.70c	total	-9.1837E-05	4.4999
24052.70c	total	2.5948E-03	0.3650
24053.70c	total	7.2096E-04	0.8493
24054.70c	total	1.5180E-05	7.5290
26054.70c	total	-4.5558E-04	0.8763
26056.70c	total	1.3197E-02	0.1791
26057.70c	total	7.9241E-04	0.5101
•••			
94239.70c	total	8.1218E-02	0.0919
94240.70c	total	-4.5498E-02	0.0288
94241.70c	total	7.6258E-04	0.1957
94242.70c	total	-6.0798E-05	0.0480
lwtr.10t	total	1.6518E-01	0.1716

 Total cross section sensitivities can also be thought of as the sensitivity to the atomic density

#### Observations:

- Water (hydrogen and oxygen) have the most impact on k in this system.
- Pu-239 has a significant, but smaller impact.
- Other significant, but less important, isotopes are Pu-240 and Fe-56.
- Pu-239 total sensitivity is small for a dominant fissile isotope
  - Investigate this by decomposing this into specific reactions

#### **MCNP6 Exercise 2: Sensitivities by Reaction**

- Copy ksen1.txt to ksen2.txt.
- Find sensitivities of total, capture, elastic, inelastic, and fission for H-1, light-water S(a,b), O-16, and Pu-239
  - Delete the old KSEN card and insert a new one

```
c c ### keff sensitivity cards c kopts blocksize= 5 c c c c reaction sensitivities for h-1, o-16, pu-239 c capture, elastic, inelastic, fission c ksen2 xs iso= 1001.70c lwtr.10t 8016.70c 94239.70c rxn= 1 -2 2 4 -6
```

Run the problem and analyze output.

#### **MCNP6 Exercise 2: Results**

1001.70c	total	4.7564E-01	0.0589
1001.70c	capture	-4.1980E-02	0.0110
1001.70c	elastic	5.1762E-01	0.0541
1001.70c	inelastic	0.0000E+00	0.0000
1001.70c	fission	0.0000E+00	0.0000
lwtr.10t	total	1.6518E-01	0.1716
lwtr.10t	capture	0.0000E+00	0.0000
lwtr.10t	elastic	0.0000E+00	0.0000
lwtr.10t	inelastic	1.6518E-01	0.1716
lwtr.10t	fission	0.0000E+00	0.0000
8016.70c	total	1.2197E-01	0.1225
8016.70c	capture	-1.3346E-03	0.0491
8016.70c	elastic	1.2219E-01	0.1219
8016.70c	inelastic	1.1203E-03	0.2583
8016.70c	fission	0.0000E+00	0.0000
94239.70c	total	8.1218E-02	0.0919
94239.70c	capture	-3.0413E-01	0.0076
94239.70c	elastic	-1.3872E-03	1.2795
94239.70c	inelastic	6.1685E-04	0.8563
94239.70c	fission	3.8605E-01	0.0140

Elastic scattering with H-1 and O-16 are important, as is inelastic thermal scattering with H-1 in H2O molecule.

٠

- Pu-239 fission and capture are of similar opposing magnitude, which is the cause of a lower than normal sensitivity to keff.
- Analyze Pu-239 capture and fission as function of energy.
# MCNP6 Exercise 3: Sensitivities by Energy

- Copy ksen2.txt to ksen3.txt.
- Find sensitivities of Pu-239 capture and fission as function of energy.
  - Delete the old KSEN card and insert a new one.
  - For the energy bins, use 0 to 0.625 eV, 0.625 eV to 100 keV, and 100 keV to 100 MeV as thermal, intermediate, and fast.

```
c c ### keff sensitivity cards c kopts blocksize = 5 c c c pu-239 capture and fission sensitivity for thermal, c intermediate, and fast c ksen3 xs iso = 94239.70c rxn = -2 -6 erg = 0 0.625e-6 0.1 100
```

• Run the problem and analyze output.

#### LA-UR-17-27058 70

#### **MCNP6 Exercise 3: Results**

#### 94239.70c capture

energy	range (1	MeV)	sensitivity	rel. unc.
0.0000E+00	6.2500	E-07	-2.7413E-01	0.0084
6.2500E-07	1.0000	E-01	-2.9833E-02	0.0124
1.0000E-01	1.0000	E+02	-1.7170E-04	0.0066
94239.70c fission				
energy	range (1	MeV)	sonsitivity	rel unc

51	- 9 ,	1	
0.0000E+00	6.2500E-07	3.3226E-01	0.0184
6.2500E-07	1.0000E-01	4.2493E-02	0.0556
1.0000E-01	1.0000E+02	1.1298E-02	0.1122

- Most of the effect for fission and capture are in the thermal range (as expected).
- Both thermal and intermediate Pu-239 capture and fission are of similar magnitude.
- Fast Pu-239 capture is negligible relative to Pu-239 fission.

# MCNP6 Exercise 4: Plotting Sensitivities by Energy

- Copy ksen3.txt to ksen4.txt.
- Find sensitivities of H-1 and O-16 elastic and Pu-239 capture and fission as function of energy.
  - Add KSENTAL=MCTAL to the KOPTS card.
  - Delete the old KSEN card and insert two new ones, one each for H-1/O-16 and Pu-239.
  - For the energy bins, use 13 logarithmically spaced bins from 1e-11 to 100 MeV.
- Run the problem and analyze output.
- Wait for instructions on plotting...

## MCNP6 Exercise 4: Keff Sensitivity Cards

```
С
c ### keff sensitivity cards
С
      blocksize = 5 ksental = mctal
kopts
С
c h-1 and o-16 elastic scatter sensitivity with energy binning
С
ksen41 xs iso = 1001.90c 8016.80c
            rxn = 2
            erg = 1e-11 12ilog 100
С
c pu-239 capture and fission sensitivity with energy binning
С
ksen42 xs iso = 94239.80c
            rxn = -2 -6
            erg = 1e-11 12ilog 100
```

#### **MCNP6 Exercise 4: Results**

sensitivity profile 41

. . .

1001.90c elastic

energy	range (MeV)	sensitivity	rel. unc.
1.0000E-11	1.0000E-10	0.0000E+00	0.0000
1.0000E-10	1.0000E-09	0.0000E+00	0.0000
1.0000E-09	1.0000E-08	0.0000E+00	0.0000
1.0000E-08	1.0000E-07	0.0000E+00	0.0000
1.0000E-07	1.0000E-06	0.0000E+00	0.0000
1.0000E-06	1.0000E-05	-6.9528E-04	3.6614
1.0000E-05	1.0000E-04	2.2688E-02	0.5444
1.0000E-04	1.0000E-03	4.2921E-02	0.2324
1.0000E-03	1.0000E-02	2.9246E-02	0.5258
1.0000E-02	1.0000E-01	6.0654E-02	0.1942
1.0000E-01	1.0000E+00	1.6379E-01	0.0729
1.0000E+00	1.0000E+01	1.7440E-01	0.0411
1.0000E+01	1.0000E+02	2.8604E-04	0.5676

# **Exercise 4: Plotting**

• To plot the ksen tallies, invoke the tally plotter and read in the mctal formatted ksental file

mcnp6 z
mcplot> rmctal ksental

- By default, the plot will contain the sensitivity profile from the first listed tally with the first isotope and reaction. In this case, the H-1 elastic scattering sensitivity is plotted.
- In general, when plotting sensitivity profiles the following commands are recommended:

logli	.n		has plot on log-lin scale
letha	rgy		changes to per lethargy normalization
xlim	1.e-11	1.e+2	sets the x-range of the plot window
ylim	-1.e-1	1.e-1	sets the y-range of the plot window

#### **Exercise 4: Plotting**

#### • The H-1 elastic scattering sensitivity profile



#### keff sensitivities to nuclear data.

• How to switch between tallies, isotopes, reactions?

# MCNP6 Exercise 4: Plotting

- From the MCNP6 manual on plotting ksen profiles from the ksental file
  - The s bin refers to the isotope bin
  - The m bin refers to the reaction bin
- The isotope/reaction bins are ordered as listed in the input:

ksen41 xs iso = 1001.90c 8016.80c rxn = 2 erg = 1e-11 12ilog 100

- For tally 41, the s=1 bin is 1001.90c and the s=2 bin is 8016.80c

For tally 42, the m=1 bin is -2 (capture) and the m=2 bin is -6 (fission)

## MCNP6 Exercise 4: Plotting

More plotting commands to switch between tallies, isotopes and reactions:

tally 42	specifies the ksen42 tally to plot			
fixed s 2	fixes the s bin to the 2 <sup>nd</sup> isotope			
fixed m 4	fixes the m bin to the 4 <sup>th</sup> reaction			

• Try the following sequence of commands to plot multiple sensitivity profiles together:

tal 41 fix s 1 lab "H-1 elastic" coplotksen41, 1st isotal 41 fix s 2 lab "O-16 elastic" coplotksen41, 2nd isotal 42 fix m 1 lab "Pu-239 capture" coplotksen42, 1st rxntal 42 fix m 2 lab "Pu-239 fission"ksen42, 2nd rxn

#### **Exercise 4: Plotting**

#### All sensitivities

Tally/lethargy/particle



keff sensitivities to nuclear data.

#### LA-UR-17-27058 79

# MCNP6 - KSEN with Secondary Distributions

More complete KSEN:

```
KSENj XS

ISO = ZAID1 ZAID2 ...

RXN = MT1 MT2 ...

ERG = E1 E2 ...

COS = C1 C2 ...

EIN = I1 I2 ...

CONSTRAIN = YES/NO
```

- Comments:
  - For secondary distributions ERG is with respect to outgoing energies (default 0 to infinity).
  - COS defines direction cosine changes from the collision (default -1 to 1)
  - EIN defines the incident energy range (default 0 to infinity)
  - CONSTRAIN tells MCNP whether the distribution must be renormalized to preserve probability (default is YES)
  - If cross sections or fission nu listed in RXN, MCNP will calculate those as normal.

# MCNP6 - Constrained Chi Sensitivity Example

#### • KSEN card of Pu-239 chi sensitivity:

ksen94	XS	iso= 94239.70c
		rxn= -1018
		erg= 1e-11 999ilog 20
		ein= 0 19i 20
		constrain= yes

#### • Comments:

- Fine outgoing energy binning in lethargy
- Incident energy bins are in 1 MeV intervals from 0 to 20 MeV
- MCNP should give a sensitivity to a distribution that is renormalized

# **Constrained Chi Sensitivity Example**

#### • Pu-239 chi sensitivity in Jezebel (Pu Sphere):



# Covariance Data

# Nuclear Data

- "Nuclear" data involves interactions of incident particles with the nucleus.
  - Data libraries include cross-section and scattering data with interpolation laws, various parameters, etc., derived from both experiments and theory
  - Typically there are "ladders" of  $(E_J, \sigma_J)$  pairs, but many other formats are also used.

 Results obtained from a calculation depend upon both the <u>code</u> and the <u>nuclear data</u> it employs

- Along with the evaluated nuclear cross sections, angular distributions, energy spectra, etc., the <u>uncertainties</u> of the nuclear data can be a large source of the overall uncertainty in any application
  - Both experimental and theoretical uncertainties contribute to the evaluated nuclear data uncertainties
  - The uncertainties are given in the form of a <u>covariance matrix</u>

# U<sup>235</sup> Fission Cross-section



# Pu<sup>239</sup> Prompt Fission Neutron Spectrum



#### How is the nuclear data determined?

### **ENDF/B & Other Libraries**

#### • ENDF/B

- In the early 1960s, the Cross Section Evaluation Working Group (CSEWG) was founded to generate reliable nuclear data
- CSEWG continues to produce and maintain the Evaluated Nuclear Data File (ENDF)
- ENDF/B-VI.0 was released in 1990, ENDF/B-VI.8 in 2000
- ENDF/B-VII.0 was released in December 2006
   ENDF/B-VII.1 was released in December 2011

   (Included upgraded covariance matrix evaluations)
- ENDF/B-VIII.0 is targeted for release in December 2017

#### Other Libraries

- JEF Joint European File
- JENDL Japanese Evaluated Nuclear Data Library
- CENDL Chinese Evaluated Nuclear Data Library
- BROND Russian
- ENDL Livermore National Laboratory
- EFF European File Fusion
- FENDL Fusion Evaluated Nuclear Data Library
- UK Nuclear Data Library

#### **Cross-section Covariance Data** (1)

• For a given isotope, these 12 cross-sections & sensitivities are used within Whisper:

MT	reaction
2	elastic scatter
4	inelastic
16	n,2n
18	fission
102	n,γ
103	n,p
104	n,d
105	n,t
106	n,³He
107	n,α
452	ν
1018	χ

## **Cross-section Covariance Data** (2)

- MCNP uses continuous-energy cross-section data & collision physics, but sensitivity profiles are tallied in 44 energy bins
- The 44 energy bins reflect the cross-section covariance data files obtained for each isotope & reaction from the BLO data (low-fidelity covariance data from the Brookhaven-LANL-ORNL covariance project)

#### **Energy bin bounds (MeV)**

1.0000e-11	3.0000e-09	7.5000e-09	1.0000e-08	2.5300e-08	3.0000e-08
4.0000e-08	5.0000e-08	7.0000e-08	1.0000e-07	1.5000e-07	2.0000e-07
2.2500e-07	2.5000e-07	2.7500e-07	3.2500e-07	3.5000e-07	3.7500e-07
4.0000e-07	6.2500e-07	1.0000e-06	1.7700e-06	3.0000e-06	4.7500e-06
6.0000e-06	8.1000e-06	1.0000e-05	3.0000e-05	1.0000e-04	5.5000e-04
3.0000e-03	1.7000e-02	2.5000e-02	1.0000e-01	4.0000e-01	9.0000e-01
1.4000e+00	1.8500e+00	2.3540e+00	2.4790e+00	3.0000e+00	4.8000e+00
6.4340e+00	8.1873e+00	2.0000e+01			

 When better cross-section covariance data become available, more energy bins will be used

#### **Cross-section Covariance Data** (3)

For a particular isotope & particular reaction (MT), the nuclear data ٠ uncertainties are a G x G matrix, where G = number of energy groups = 44



44 energy bins  $\rightarrow$ 

- Each diagonal is the variance of the cross-section for a particular energy bin
- Off-diagonal elements are the shared variance between the data for pairs of energy bins

# Cross-section Covariance Data (4)



FIG. 9: A typical NJOY-generated plot of ENDF/B-VII.0 data downloaded from the National Nuclear Data Center, BNL, USA.

## **Cross-section Covariance Data** (5)



FIG. 3: Correlation matrix for the neutron-induced fission cross section on  $^{235}$ U. It was evaluated by Pronyaev *et al.* as part of the cross section standards evaluation [19].





FIG. 13:  $^{238}\mathrm{U}$  fission cross-section correlation matrix.

Covariance plots on this & next page taken from:

P. Talou, P.G. Young, T. Kawano, M. Rising, M.B. Chadwick, "Quantification of Uncertainties for Evaluated Neutron-Induced Reactions on Actinides in the Fast Energy Range", Nuclear Data Sheets 112, 3054–3074 (2011)



#### Sensitivity-Uncertainty Techniques for Nuclear Criticality Safety

#### **Cross-section Covariance Data** (6)







FIG. 25: Correlation matrix evaluated for the <sup>238</sup>Pu (n,fission) cross section.

FIG. 40: Correlation matrix evaluated for the n(0.5)MeV)+<sup>239</sup>Pu prompt fission neutron spectrum.

FIG. 43: Evaluated correlation matrix for the neutroninduced fission cross section of <sup>240</sup>Pu in the fast energy range.





0.2 0.6 0.8 0.4 0 1  $10^{1}$ Energy (MeV) 10<sup>0</sup>  $10^{-1}$  $10^{-1}$  $10^{0}$ 10<sup>1</sup> Energy (MeV)

FIG. 45: <sup>240</sup>Pu (n,total) cross section correlation matrix.

FIG. 47: Correlation matrix for the  $n+^{240}$ Pu capture cross section. Large off-diagonal elements are due mostly to model uncertainties, since no experimental data exist above 300 keV.

Energy (MeV)



## **Cross-section Covariance Data** (7)

• For each isotope, with 44 energies & 12 reactions:

 $C_{xx}^{lso}$ : c(44, 44, 12, 12)

- Each diagonal element of  $C_{xx}$  is the variance of the cross-section for a particular MT & energy bin
- Off-diagonal elements of C<sub>xx</sub> are the shared variance between pairs of MT-E & MT'-E' (Off-diagonal MT-MT' blocks would generally be 0)



- Each  $C_{xx}^{lso}$  entry is produced by SCALE or NJOY based on covariance data from the ENDF/B libraries (with some adjustments if needed)
- The  $C_{xx}$  data is universal, independent of benchmark or application problem

#### **Cross-section Covariance Data** (8)

 The covariance matrices for all isotopes can be combined, including offdiagonal blocks that relate uncertainties in one iso-MT-E with a different iso-MT-E



- Each diagonal element of  $C_{xx}$  is the variance of the cross-section for a particular isotope, MT, & energy bin
- Off-diagonal elements of C<sub>xx</sub> are the shared variance between pairs of Iso-MT-E & Iso'-MT'-E'
- Very sparse (lots of zeros), block-structured matrix (Off-diagonal I-I' blocks would generally be zero)

## **Sensitivity Profiles (Vectors)**

- For each isotope, the sensitivity coefficients for a specific problem are stored consistent with the layout of the covariance data
  - Recall that the sensitivity of Keff to a particular reaction type & energy bin is:

$$S_{k,x} = \frac{\Delta k/k}{\Delta x/x} = \frac{x}{k} \frac{dk}{dx}$$

where x is the cross-section for a particular isotope, reaction, & energy bin



 For a particular application problem, A, the sensitivity profiles for all isotopes are combined into one sensitivity vector S<sub>A</sub>



# **Correlation Coefficients**

# **Correlation Coefficient (1)**

- Correlation coefficient
  - Pearson product-moment correlation coefficient, r or  $\rho$
  - A measure of the linear correlation between variables X & Y
    - $\rho = +1$  total positive correlation
    - $\rho = -1$  total negative correlation
    - $\rho = 0$  no correlation



# **Correlation Coefficient (2)**

- Population correlation coefficient,  $\rho$ 
  - Distribution of X, with mean  $\mu_x$ , standard deviation  $\sigma_x$
  - Distribution of Y, with mean  $\mu_v$ , standard deviation  $\sigma_v$

$$\rho_{X,Y} = \frac{\operatorname{cov}(X,Y)}{\sigma_X \cdot \sigma_Y} = \frac{E[(X - \mu_X)(Y - \mu_Y)]}{\sigma_X \cdot \sigma_Y} = \frac{E(XY) - E(X) \cdot E(Y)}{\sigma_X \cdot \sigma_Y}$$

$$\mu_X = E(X) \qquad \sigma_X^2 = E[(X - E(X))^2] = E(X^2) - E(X)^2$$
  
$$\mu_Y = E(Y) \qquad \sigma_Y^2 = E[(Y - E(Y))^2] = E(Y^2) - E(Y)^2$$

- Sample correlation coefficient, r
  - Dataset for X: {  $x_1, x_2, \dots, x_n$  }, mean x-bar, std dev  $s_x$
  - Dataset for Y: {  $y_1$ ,  $y_2$ , ....,  $y_n$  } mean y-bar, std dev  $s_v$

$$r = r_{xy} = \frac{\frac{1}{n}\sum x_i y_i - \overline{x} \cdot \overline{y}}{s_x \cdot s_y}$$

# Variance in Keff & Correlation Between Problems

- Given: Problem A, Sensitivity S<sub>A</sub> computed by MCNP Problem B, Sensitivity S<sub>B</sub> computed by MCNP
- Variance in Keff due to nuclear data uncertainties:

$$Var_{k}(A) = \vec{S}_{A}\vec{C}_{xx}\vec{S}_{A}^{T}$$
$$Var_{k}(B) = \vec{S}_{B}\vec{C}_{xx}\vec{S}_{B}^{T}$$



Covariance between A & B due to nuclear data uncertainties:

$$Cov_k(A,B) = \vec{S}_A \vec{C}_{xx} \vec{S}_B^T$$

• Correlation between Problems A & B due to nuclear data:

$$c_{k}(A,B) = \frac{Cov_{k}(A,B)}{\sqrt{Var_{k}(A)} \cdot \sqrt{Var_{k}(B)}} = \frac{\vec{S}_{A}\vec{C}_{xx}\vec{S}_{B}^{T}}{\sqrt{\vec{S}_{A}\vec{C}_{xx}}\vec{S}_{A}^{T} \cdot \sqrt{\vec{S}_{B}\vec{C}_{xx}}\vec{S}_{B}^{T}}$$

# Sandwich Rule – Variance & Covariance



**Error Propagation (1)** 

Define a linear relationship

$$\mathbf{y} = \mathbf{A}\mathbf{x} + \mathbf{b}$$

• Determine expected (mean) value of y

$$\mu_{\mathbf{y}} = E[\mathbf{y}] = E[\mathbf{A}\mathbf{x} + \mathbf{b}] = \mathbf{A}E[\mathbf{x}] + \mathbf{b} = \mathbf{A}\mu_{\mathbf{x}} + \mathbf{b}$$

• Determine covariance matrix of y

$$\mathbf{C}_{\mathbf{y}} = \operatorname{cov}(\mathbf{y}, \mathbf{y}) = E[(\mathbf{y} - \mu_{\mathbf{y}})(\mathbf{y} - \mu_{\mathbf{y}})^{T}]$$
  

$$= E[(\mathbf{A}\mathbf{x} + \mathbf{b} - \mathbf{A}\mu_{\mathbf{x}} - \mathbf{b})(\mathbf{A}\mathbf{x} + \mathbf{b} - \mathbf{A}\mu_{\mathbf{x}} - \mathbf{b})^{T}]$$
  

$$= E[(\mathbf{A}(\mathbf{x} - \mu_{\mathbf{x}}))(\mathbf{A}(\mathbf{x} - \mu_{\mathbf{x}}))^{T}]$$
  

$$= E[\mathbf{A}(\mathbf{x} - \mu_{\mathbf{x}})(\mathbf{x} - \mu_{\mathbf{x}})^{T}\mathbf{A}^{T}]$$
  

$$= \mathbf{A} E[(\mathbf{x} - \mu_{\mathbf{x}})(\mathbf{x} - \mu_{\mathbf{x}})^{T}]\mathbf{A}^{T}$$
  

$$= \mathbf{A} \operatorname{cov}(\mathbf{x}, \mathbf{x})\mathbf{A}^{T}$$
  

$$\mathbf{C}_{\mathbf{y}} = \mathbf{A} \mathbf{C}_{\mathbf{x}}\mathbf{A}^{T} \checkmark$$
 "Sandwich" Rule

**Error Propagation (2)** 

• First-order Taylor series expansion of k about cross section, Σ

$$k(\Sigma_1', \Sigma_2', \dots, \Sigma_N') \cong k(\Sigma_1^0, \Sigma_2^0, \dots, \Sigma_N^0) + \sum_{i=1}^N \frac{\partial k}{\partial \Sigma_i} \bigg|_{\Sigma_i^0} (\Sigma_i' - \Sigma_i^0)$$

• Define vectors for cross sections and sensitivity profiles

$$\begin{split} \vec{\Sigma}' &= \begin{bmatrix} \Sigma_1' & \Sigma_2' & \cdots & \Sigma_N' \end{bmatrix} \\ \vec{\Sigma}^0 &= \begin{bmatrix} \Sigma_1^0 & \Sigma_2^0 & \cdots & \Sigma_N^0 \end{bmatrix} \\ \vec{\Sigma}^0 &= \begin{bmatrix} \Sigma_1^0 & \Sigma_2^0 & \cdots & \Sigma_N^0 \end{bmatrix} \\ \vec{\Sigma}^0 &= \begin{bmatrix} \Sigma_1^0 & \Sigma_2^0 & \cdots & \Sigma_N^0 \end{bmatrix}$$

• Determine covariance matrix (variance) of k

$$k(\overline{\Sigma}') \cong k(\overline{\Sigma}^{0}) + \overline{S} (\overline{\Sigma}' - \overline{\Sigma}^{0})^{T}$$
$$= \overline{S} \,\overline{\Sigma}'^{T} + \left[ k(\overline{\Sigma}^{0}) - \overline{S} \,\overline{\Sigma}^{0T} \right]$$
$$= \mathbf{A}\mathbf{x} + \mathbf{b}$$

$$\mathbf{C}_{k} = \vec{S} \, \mathbf{C}_{\Sigma} \, \vec{S}^{T}$$
Sensitivity-Uncertainty Techniques for Nuclear Criticality Safety

#### **Error Propagation (3)**

• Example using sandwich rule, <sup>239</sup>Pu PFNS impact on *k* 



# **MCNP-WHISPER**

# for Nuclear Criticality Safety Validation

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LANL PF4 Restart

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#### Whisper – Summary

#### Whisper - Software for Sensitivity-Uncertainty-Based Nuclear Criticality Safety Validation

Whisper is computational software designed to assist the nuclear criticality safety (NCS) analyst with validation studies with the Monte Carlo radiation transport package MCNP. Standard approaches to validation rely on the selection of benchmarks based upon expert judgment. Whisper uses sensitivity/uncertainty (S/U) methods to select relevant benchmarks to a particular application or area of applicability (AOA), or set of applications being analyzed. Using these benchmarks, Whisper computes a calculational margin from an extreme value distribution. In NCS, a margin of subcriticality (MOS) that accounts for unknowns about the analysis. Typically, this MOS is some prescribed number by institutional requirements and/or derived from expert judgment, encompassing many aspects of criticality safety. Whisper will attempt to quantify the margin from two sources of potential unknowns, errors in the software and uncertainties in nuclear data. The Whisper-derived calculational margin and MOS may be used to set a baseline upper subcritical limit (USL) for a particular AOA, and additional margin may be applied by the NCS analyst as appropriate to ensure subcriticality for a specific application in the AOA.

Whisper provides a benchmark library containing over 1,100 MCNP input files spanning a large set of fissionable isotopes, forms (metal, oxide, solution), geometries, spectral characteristics, etc. Along with the benchmark library are scripts that may be used to add new benchmarks to the set; this documentation provides instructions for doing so. If the user desires, Whisper may analyze benchmarks using a generalized linear least squares (GLLS) fitting based on nuclear data covariances and identify those of lower quality. These may, at the discretion of the NCS analyst and their institution, be excluded from the validation to prevent contamination of potentially low quality data. Whisper provides a set of recommended benchmarks to be optionally excluded.

Whisper also provides two sets of 44-group covariance data. The first set is the same data that is distributed with SCALE 6.1 in a format that Whisper can parse. The second set is an adjusted nuclear data library based upon a GLLS fitting of the benchmarks following rejection. Whisper uses the latter to quantify the effect of nuclear data uncertainties within the MOS. Whisper also has the option to perform a nuclear covariance data adjustment to produce a custom adjusted covariance library for a different set of benchmarks.

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#### Whisper

- Whisper History, Background, SQA Status, Documentation
- Whisper Methodology
  - Capabilities
  - Correlation Coefficients
  - Cross-section Covariance Data
  - Sensitivity Profiles
  - Variance in Keff & Correlation Between Problems
  - Determining benchmark C<sub>k</sub>'s
  - Determining bias & bias uncertainty
  - Determining portions of the MOS
- Using Whisper for Validation
  - Overview
  - Using whisper\_mcnp
  - Using whisper\_usl
  - Examples

#### MCNP-WHISPER Methodology for Nuclear Criticality Safety Analysis

- Nuclear Criticality Safety requires validation of computational methods
- Validation involves comparing calculation vs experiment for many benchmarks similar to the application of interest
- Neutron spectra are complex functions of geometry, materials, nuclear crosssections. etc.
- Simple metrics cannot capture the complexity of a fissile system
- During the past 20 years, a powerful set ٠ of tools has been developed based on sensitivity-uncertainty methods



#### MCNP-WHISPER Methodology for Nuclear Criticality Safety Validation

- **MCNP** determines sensitivity profiles to characterize the neutronics of an application or benchmark, S( energy, reaction, isotope ),  $S = (dk/k) / (d\sigma/\sigma)$
- WHISPER uses sensitivity profiles & data covariances to select similar benchmarks, determine bias, bias-uncertainty, & margin-of-subcriticality for setting the **Upper-Subcritical-Limit (USL)**



#### MCNP-WHISPER Methodology for Nuclear Criticality Safety Analysis (2)

 The sensitivity coefficient is the ratio of relative change in k-effective to relative change in a system parameter:

$$\boldsymbol{S}_{\boldsymbol{k},\boldsymbol{x}} = \frac{\boldsymbol{d}\boldsymbol{k}/\boldsymbol{k}}{\boldsymbol{d}\boldsymbol{x}/\boldsymbol{x}} = -\frac{\left\langle \boldsymbol{\psi}^{\dagger}, \left(\boldsymbol{\Sigma}_{\boldsymbol{x}} - \boldsymbol{S}_{\boldsymbol{x}} - \boldsymbol{k}^{-1}\boldsymbol{F}_{\boldsymbol{x}}\right)\boldsymbol{\psi} \right\rangle}{\left\langle \boldsymbol{\psi}^{\dagger}, \boldsymbol{k}^{-1}\boldsymbol{F}\boldsymbol{\psi} \right\rangle}$$

- $S_{k,x}(E)$  is the sensitivity profile, that includes all isotopes, reactions, & energies for a system:
- MCNP Monte Carlo uses the Iterated Fission Probability method to compute adjoint-weighted integrals for the sensitivity profiles
  - Tally scores are collected in original generation, adjoint-weighting is based on the progeny in the asymptotic generation



#### MCNP-WHISPER Methodology for Nuclear Criticality Safety Analysis (3)



#### Whisper Methodology for Validation & USLs

- Whisper
  - Statistical analysis code to determine baseline USLs
  - Uses sensitivity profiles from continuous-energy MCNP6
  - Uses covariance data for nuclear cross-sections
- Using Whisper

Run MCNP6 for an Application, & get Application sensitivity profile,  $S_A$  Run Whisper:

- ① Automated, physics-based selection of benchmarks that are neutronically similar to the application, ranked & weighted
  - Compare Application  $S_A$  to each of the Benchmark sensitivities  $S_{B(i)}$
  - Select most-similar benchmarks (highest  $S_A$ - $S_{B(i)}$  correlation coefficients)
- **②** Bias + bias uncertainty from Extreme Value Theory
  - Statistical analysis based on most-similar Benchmarks selected

#### ③ Margin for nuclear data uncertainty estimated by GLLS method

 Use benchmark sensitivities & cross-section covariance data to estimate the MOS for nuclear data uncertainties

## **MCNP6 & Whisper Status**

MCNP releases by RSICC

MCNP6.1 – 2013, production version
MCNP6.1.1 – 2014, same criticality, faster, beta features for DHS
MCNP6.2 – 2017 (Fall), with Whisper code & benchmarks

ENDF/B-VII.1 data, updates, & older data Reference Collection  $-700^+$  technical reports V&V Test Collection -1434 test problems

#### • Whisper-1.1.0 (2016)

[original Whisper-1.0.0 (2014)]

- SQA
  - Whisper is now part of MCNP6, rigorous SQA
  - Portable to Linux, Mac, & Windows, same results
- Benchmark Suite
  - 1101 ICSBEP benchmarks, with sensitivity profiles from MCNP6 for all isotopes & reactions
- Software
  - Available to any DOE crit-safety group
  - Will be included with MCNP6.2 release (Fall 2016)
- Documentation

mcnp.lanl.gov  $\rightarrow$  "Reference Collection"  $\rightarrow$  "Whisper – NCS Validation"

## Whisper SQA

- Whisper is part of the MCNP software package
  - Will be distributed to the criticality-safety community via future RSICC releases of MCNP
  - Feedback from criticality-safety analysts at DOE sites will be factored into future development
  - Potential for world-wide feedback/review/improvements
- Maintained under MCNP version control system (GIT, TeamForge)
  - LANL standard
  - WHISPER GIT Module for checkout into MCNP source tree
  - All revisions, additions, improvements tracked under Artifact 36407
- MCNP SQA methodology
  - Encompasses Whisper
  - Previous audits & reviews of MCNP SQA determined that methodology was compliant with DOE/ASC & LANL P1040 requirements
  - Review is in progress to assess current MCNP SQA P1040 compliance, and make any revisions required to continue compliance
  - P1040 compliance implies DOE-414.1D compliance, hence standards

# Whisper Methodology

#### Whisper

#### **Whisper Methodology**

- MCNP6
  - Determine Sensitivity Profiles for Benchmarks B<sub>1</sub> ... B<sub>N</sub>
  - Determine Sensitivity Profiles for Application A
- Whisper Determine Benchmark c<sub>k</sub>'s
  - For each benchmark  $B_J$ , determine  $c_k^{(J)}$  correlation coefficient between A &  $B_J$

#### - Whisper - Determine Benchmark Weights & Select Benchmarks

• Iterative procedure using  $c_k^{(J)}$  values,  $c_{k,max}$ ,  $c_{k,acc}$ 

#### - Whisper - Determine Calculational Margin (CM)

- Extreme Value Theory, with weighted data, nonparametric
- Compute bias & bias uncertainty
- Adjustment for non-conservative bias
- Handling small sample sizes

#### Whisper – Determine portions of MOS

#### Whisper Capabilities

#### Admin

- Install code, scripts, benchmarks, covariance files, correlations
- Test the installation
- Identify inconsistent benchmarks to be rejected
- Estimate missing benchmark uncertainties
- Can add additional benchmarks
- Can reject additional benchmarks

#### User

 Use whisper\_mcnp script to run MCNP6 for process models, to obtain k<sub>eff</sub> & sensitivity profiles for all isotopes & reactions

 Use whisper\_usl script to run Whisper for process models

- Whisper matches process model sensitivity profiles with benchmark library profiles, selects most similar benchmarks
- Compute calculational margin for each process model, based on selected benchmarks (bias + bias uncertainty)
- Estimate cross-section portion of MOS based on GLLS
- Use 0.005 for code unknowns portion of MOS
- Estimate baseline USL for each process model (not including additional AOA or other margin)

#### **Using Whisper for Validation**

- As part of Whisper installation (not day-to-day use),
  - For each of the 1100+ benchmarks
    - MCNP6 is run to generate the sensitivity vector  $S_B$  for that benchmark
    - The sensitivity vector  $S_B$  for each benchmark is saved in a folder
  - The nuclear data covariance files are saved in a folder
  - Benchmarks are checked for consistency, some may be rejected
  - Missing uncertainties for some benchmarks are estimated
  - Details will be covered later. All of this is the responsibility of the Admin person & needs to be done only once at installation (or repeated if the code, data, or computer change)
- To use Whisper for validation:
  - Use the whisper\_mcnp script to make 1 run with MCNP6 for a particular application, to generate the sensitivity vector for the application,  $S_A$
  - Run Whisper, using the whisper\_usl script

#### Whisper – Overview of Application Use

- Given S<sub>A</sub> for an application, the nuclear data covariance files, and the collection of 1100+ S<sub>B</sub> vectors for the benchmarks
  - For each of the benchmarks, compute the correlation between the benchmark & application problem,  $c_k(A,B)$
  - Use the  $c_k(A,B)$  values for the benchmarks to compute relative weights for each benchmark
  - Select the a set of benchmarks with the highest weights (i.e., the highest neutronics correlations between benchmarks & application)
  - Using the selected benchmarks, compute bias, bias uncertainty, & extra margin based on nuclear data uncertainty
  - There are of course details, such as acceptable c<sub>k</sub> values, determining weights using c<sub>k</sub> values, extra penalty if not enough similar benchmarks, benchmark correlation, .....

#### Whisper Details – Compute c<sub>k</sub> Values

- Given:
  - Problem A, Application Sensitivity S<sub>A</sub> computed by MCNP
  - Problem  $B_J$ , Benchmark Sensitivity  $S_{Bj}$  computed by MCNP, J = 1, ..., N (N = number of benchmarks)
- Find correlation between Application A & Benchmark B<sub>J</sub>, J = 1 ... N:

$$c_{k}^{(J)}(A,B_{J}) = \frac{Cov_{k}(A,B_{J})}{\sqrt{Var_{k}(A)} \cdot \sqrt{Var_{k}(B_{J})}} = \frac{\bar{S}_{A}\bar{C}_{xx}\bar{S}_{B_{J}}^{T}}{\sqrt{\bar{S}_{A}\bar{C}_{xx}\bar{S}_{A}^{T}} \cdot \sqrt{\bar{S}_{B_{J}}\bar{C}_{xx}\bar{S}_{B_{J}}^{T}}}$$

Eliminate any negative correlation coefficients

- If 
$$c_k^{(J)} < 0$$
, set  $c_k^{(J)} = 0$ ,  $J = 1 ... N$ 

• Determine maximum  $c_k^{(J)}$ ,  $c_{k,max}$ 

#### Whisper Details – Benchmark Weights (1)

- Benchmarks are assigned weights  $w_J$  based on their  $c_k^{(J)}$  values,  $c_{k,max}$ , and a (to-be-determined) acceptance threshold,  $c_{k,acc}$ 
  - Benchmarks similar to the application,  $c_k^{(J)} > c_{k,acc}$ :  $0 < w_J \le 1$
  - Benchmarks <u>not</u> similar to the application,  $c_k^{(J)} < c_{k,acc}$ :
  - Scheme for determining w<sub>J</sub> is on next slide
- The <u>minimum required total weight</u>, w<sub>req</sub>, for the set of selected benchmarks is:

$$\begin{split} w_{req} &= w_{min} + (1 - c_{k,max})^* w_{penalty} \\ where & w_{min} &= 25 \\ w_{penalty} &= 100 \end{split} \begin{tabular}{ll} (default, user opt) \\ (default, user opt) \end{array}$$

That is, must select enough benchmarks so that sum{  $w_J$  } ≥  $w_{req}$  Rationale

- 25 or more are needed for reliable statistical treatment
- If benchmarks are <u>not</u> close to application (c<sub>k,max</sub> not close to 1.0), want to require more of them. Simple linear penalty.

 $W_{.1} = 0$ 

#### Whisper Details – Benchmark Weights (2)

- The determination of benchmark weights is iterative, based on an acceptance criteria c<sub>k,acc</sub>
  - c<sub>k,acc</sub> is the minimum <u>threshold</u> for c<sub>k</sub><sup>(J)</sup> values
  - Benchmarks with  $c_k^{(J)} < c_{k,acc}$  are assigned  $w_J = 0$
  - Benchmarks with  $c_k^{(J)} \ge c_{k,acc}$  are assigned weight

$$\boldsymbol{W}_{J} = \frac{\boldsymbol{C}_{k}^{(J)} - \boldsymbol{C}_{k,acc}}{\boldsymbol{C}_{k,max} - \boldsymbol{C}_{k,acc}}$$

- Iterative procedure determines largest c<sub>k,acc</sub> that satisfies requirement that sum{ w<sub>J</sub> } ≥ w<sub>req</sub>
  - Select a value for  $c_{k,acc}$  close to  $c_{k,max}$
  - Determine benchmark weights (by above scheme)
  - If  $sum\{w_J\} < w_{req}$ , decrease  $c_{k,acc}$  by 10<sup>-5</sup> & repeat above step
  - The iteration ends when enough benchmarks with highest  $w_J$ 's are selected so that  $sum{w_J} \ge w_{req}$

If not enough benchmarks to satisfy total weight requirement, adjustment scheme is used. Discussed later, at end.....

#### Whisper Details – Calculational Margin (1)

- Whisper uses a nonparametric statistical approach to determining the calculational margin (bias + bias uncertainty)
  - Does not rely on assumption that (k<sub>calc</sub> k<sub>bench</sub>) is normally distributed for the set of benchmarks
  - Can handle weighted benchmarks (Tsunami rank-order scheme can't)
  - Based on Extreme Value Theory
    - The addition of less-relevant benchmarks cannot reduce the calculational margin
    - Irrelevant benchmarks (i.e., low c<sub>k</sub>) will not non-conservatively affect results
    - Accounting for weighting avoids overly conservative calculational margin
- Whisper uses EVT to to find the value of a calculational margin that bounds the worst-case bias to some probability of a weighted population

Note in following discussion:

- There is the fundamental assumption that for a single benchmark, the bias for that benchmark is normally distributed, according to the experimental uncertainty & Monte Carlo statistics
- There is no assumption of normality across the collection of benchmarks, however. The method is nonparametric.

#### Whisper Details – Calculational Margin (2)

- Let  $\beta_J = k_{calc J} k_{bench J}$  and  $\sigma^2_J = \sigma^2_{bench J} + \sigma^2_{calc J}$ 
  - For convenience, the  $X_J\,$  below are opposite in sign to  $\beta_J$
- For a set of N benchmarks, let  $X_J$  be a random variable normally distributed about  $\beta_J$  with uncertainty  $\sigma_J$ . The cumulative distribution function (CDF) for  $X_J$  is

$$F_{j}(x) = \operatorname{Prob}(X_{j} < x) = \frac{1}{\sqrt{2\pi} \cdot \sigma_{j}} \int_{-\infty}^{x} \exp\left[-\frac{1}{2}\left(\frac{y+\beta_{j}}{\sigma_{j}}\right)^{2}\right] dy = \frac{1}{2}\left[1 + \operatorname{erf}\left(\frac{x+\beta_{j}}{\sqrt{2\sigma_{j}^{2}}}\right)\right]$$

Note:  $+\beta_J$ , due to opposite sign

• Let the random variable X be the maximum (opposite-signed) bias for the benchmark collection:

$$X = max\{ X_1, ..., X_N \}$$

• The cumulative distribution function (CDF) for X is

$$F(x) = \operatorname{Prob}(X \leq x) = \prod_{J=1}^{N} F_J(x)$$

#### LA-UR-17-27058 127

## Whisper Details – Calculational Margin (3)

• When benchmarks are <u>weighted</u>, the following form is used for  $F_J(x)$ 

$$F_{j}(x) = (1 - w_{j}) + \frac{w_{j}}{2} \left[ 1 + \operatorname{erf}\left(\frac{x + \beta_{j}}{\sqrt{2\sigma_{j}^{2}}}\right) \right]$$

- For all benchmarks J = 1, ..., N, Whisper computes
  - Benchmark weight,
     w<sub>J</sub>
  - Bias,  $\beta_J$
  - Bias uncertainty,  $\sigma_J$
- Those quantities & the weighted  $F_J(x)$  determine F(x):

 $F(x) = \prod_{J=1}^{N} F_{J}(x)$ 

 Whisper determines the calculational margin (bias + bias uncertainty) by numerically solving:

F(CM) = .99 (.99 is default, user opt)

CM is the calculational margin that bounds the worst-case benchmark bias & bias uncertainty with probability .99 (default)

#### Whisper Details – Calculational Margin (4)

- Bias & bias uncertainty
  - USL = 1 CM MOS
    - = 1 + bias bias-uncert  $\Delta_{non-conserv}$  MOS
  - ANSI/ANS-8.24:

"Individual elements (e.g., bias and bias uncertainty) of the calculational margin need not be computed separately. Methods may be used that combine the elements into the calculational margin."

- Whisper computes CM by numerically solving F(CM) = .99
- Whisper computes bias & bias uncertainty numerically as:

bias 
$$= -\int_{-\infty}^{\infty} x \cdot f(x) dx = -\int_{-\infty}^{\infty} x F(x) \sum_{J=1}^{N} w_J \frac{f_J(x)}{F_J(x)} dx$$
  
 $\sigma_{\text{bias}} = CM + \text{bias}$ 

 If the bias is non-conservative (positive), then the CM is adjusted so that no credit is taken for non-conservative bias

if bias>0, CM = CM + bias

#### Whisper Details – Calculational Margin (5)

What if there are not enough benchmarks to meet the requirement that  $sum{w_J} = w_{req}$ ?

• Define these quantities:

 $W_{sum} = sum\{w_J\}$  - sum of all benchmark weights,  $w_{sum} < w_{req}$ 

- $CM_0$  = calculational margin computed with all benchmark weights set to 1.0
  - CM<sub>0</sub> is an upper bound, wide application space but not specific enough for the application being analyzed
  - Typically large & very over-conservative
- CM' = calculation margin with weighted benchmarks, but  $w_{sum} < w_{reg}$ 
  - Note that  $CM_0 \ge CM'$

• Compute CM from: 
$$CM = CM' \cdot \frac{W_{sum}}{W_{req}} + CM_0 \cdot \left(1 - \frac{W_{sum}}{W_{req}}\right)$$

Should question the benchmark suite,
 & include extra conservative margin of subcriticality

## Margin of Subcriticality

**MOS = MOS**<sub>software</sub> + **MOS**<sub>data</sub> + **MOS**<sub>application</sub>

- MOS = additional margin "that is sufficiently large to ensure that the calculated conditions will actually be subcritical" (ANSI/ANS-8.24)
- MOS<sub>software</sub> (for MCNP)
  - No approximations from mesh or multigroup
  - Exact answers to analytical benchmarks with given xsecs
  - Many years testing with collision physics & random sampling
  - Only realistic concern is unknown bugs
    - MCNP is used a lot, for many different criticality applications
    - Bugs that produce  $\Delta k < 0.0010$  are difficult to distinguish from data uncertainties
    - Past bugs that produced  $\Delta k > 0.0020$  are very few, but reported & fixed
    - Historical detection limit for bugs is  $\Delta k \sim 0.0020$
    - Expert judgment, conservative: MOS<sub>software</sub> = 0.0050
       → Any unknown bug larger than this would have certainly been found & fixed
    - Other MC codes should almost certainly use a larger margin
    - Analysts may use a larger number, but have no basis for a smaller number

#### Margin of Subcriticality

# **MOS = MOS**<sub>software</sub> + **MOS**<sub>data</sub> + **MOS**<sub>application</sub>

- MOS<sub>application</sub>
  - Analyst: analyses, scoping, judgment
  - Consider uncertainties in dimensions, densities, isotopics, etc.
  - Consider the number of similar benchmark cases
  - Consider area-of-applicability
  - Expert judgment, backed up by analysis

#### Margin of Subcriticality

## **MOS = MOS**<sub>software</sub> + **MOS**<sub>data</sub> + **MOS**<sub>application</sub>

#### • MOS<sub>data</sub>

- The largest portion of MOS comes from uncertainties in the nuclear cross-section data
- Data uncertainties could be as large as 0.5% 1% in extra MOS, possibly more, possibly less
- MOS<sub>data</sub> depends on the application
  - For common applications, where there are lots of benchmark experiments, the relevant ENDF/B-VII data was adjusted based on those benchmarks
  - For less common applications, where there are few benchmark experiments, ENDF/B-VII adjustments for benchmarks plays little or no role in the data
- In the past, very difficult to assess MOS<sub>data</sub>, which led to large conservative margins
- Whisper (LANL) & Tsunami (ORNL) both use essentially the same methodology to address MOS<sub>data</sub> – GLLS
- Generalized Linear Least Squares (GLLS) takes into account the experiments, calculations, sensitivities, & data covariance data to predict MOS<sub>data</sub>

#### Margin of Subcriticality - GLLS

• The goal of GLLS:

(start at the end.....)

- Determine adjustments to the nuclear data,  $\Delta x$ , which produce changes in computed k<sub>eff</sub> for benchmarks,  $\Delta k$ , such that this quantity is minimized for the set of benchmarks:

$$\chi^{2} = \Delta \vec{k} \cdot \vec{C}_{kk} \cdot \Delta \vec{k}^{T} + \Delta \vec{x} \cdot \vec{C}_{xx} \cdot \Delta \vec{x}^{T}$$

- Δk is a vector of the relative changes in the ratio of calculated k to benchmark k, due to the change in cross-section data Δx. The length of Δk is the number of benchmarks
- $\Delta x$  is a vector of the relative differences of cross-section data from their mean values. The length of  $\Delta x$  is (isotopes)\*(reacions)\*(energies)
- C<sub>kk</sub> is the relative covariance matrix for the benchmark experiment k's
  - Diagonal elements are variance of each benchmark experiment
  - Off-diagonals are correlation between benchmark measurements. (From DICE, often zero or not well-known)
- C<sub>xx</sub> is the relative covariance matrix for the nuclear data
- GLLS finds  $\Delta x$  (and the resulting  $\Delta k$ ) such that  $\chi^2$  is minimized

#### Margin of Subcriticality - GLLS

- The goal of GLLS:
  - Determine adjustments to the nuclear data,  $\Delta x$ , which produce changes in computed k<sub>eff</sub> for benchmarks,  $\Delta k$ , such that this quantity is minimized for the set of benchmarks:

$$\chi^{2} = \Delta \vec{k} \cdot \vec{C}_{kk} \cdot \Delta \vec{k}^{T} + \Delta \vec{x} \cdot \vec{C}_{xx} \cdot \Delta \vec{x}^{T}$$

- With no data adjustment,  $\Delta x = 0$ , so  $\chi^2$  determined only by differences in calculated & benchmark k's
- If data is adjusted to decrease 1<sup>st</sup> term, then 2<sup>nd</sup> term increases
- GLLS determines optimum tradeoff (minimum  $\chi^2$ ) between  $\Delta x \& \Delta k$

# Measured $k_{eff}$ values for benchmarks: $\vec{m} = (m_i), \qquad i = 1,...l \qquad (l = \# \text{ benchmarks})$

Covariance matrix for  $\vec{m}$ , relative to calculated  $k_{eff}$ 's:

$$\overline{\mathbf{C}}_{mm} = \left(\frac{m_i}{k_i} \cdot \frac{\operatorname{cov}(m_i, m_j)}{m_i m_j} \cdot \frac{m_j}{k_j}\right), \qquad i, j = 1, \dots, N$$

Covariance between measured benchmark k's (m's) & cross-section data:

$$\overline{C}_{xm} = \left(\frac{\operatorname{cov}(x_n, m_i)}{x_n m_i} \cdot \frac{m_i}{k_i}\right), \qquad n = 1, ..., M \qquad i = 1, ..., I$$

This represents correlations between cross-section data & the measured benchmark k's. At present, these data do not exist. Neither Tsunami nor Whisper use C<sub>xm</sub>.

#### GLLS

Linear changes in calculated  $k_{eff}$  due to perturbation in data,  $\vec{x}$ :

$$k_i(\vec{x}') = k_i(\vec{x} + \delta \vec{x}) = k_i(\vec{x}) + \delta k_i = k_i(\vec{x}) \cdot \left[1 + \sum_{n=1}^M S_n^{(i)} \cdot \frac{\delta x_n}{x_n}\right]$$

**Recall that:** 

Sensitivity matrix for a set of benchmarks:

$$\overline{S}_{k} = \left(\frac{X_{n}}{k_{i}} \cdot \frac{\partial k_{i}}{\partial x_{n}}\right) \qquad i = 1, ..., I \text{ (rows)} \qquad n = 1, ..., M \text{ (cols)}$$

Covariance matrix for nuclear data,  $\vec{x}$ :

$$\overline{C}_{xx} = \left(\frac{\operatorname{cov}(x_n, x_p)}{x_n x_p}\right) \qquad n = 1, ..., M \qquad p = 1, ..., M$$

Uncertainty matrix for the set of benchmarks, due to data:

$$\bar{\boldsymbol{C}}_{kk} = \bar{\boldsymbol{S}}_k \cdot \bar{\boldsymbol{C}}_{xx} \cdot \bar{\boldsymbol{S}}_k^{\mathsf{T}}$$

Express the relative changes in k for a set of benchmarks due to data perturbations:

$$\frac{k_i(\vec{x}') - m_i}{k_i(\vec{x})} = \frac{k_i(\vec{x}) - m_i}{k_i(\vec{x})} + \left[\sum_{n=1}^M S_n^{(i)} \cdot \frac{\delta x_n}{x_n}\right]$$

or

$$\vec{y} = \vec{d} + \vec{S}_k \cdot \vec{z}$$

#### LA-UR-17-27058 137

#### GLLS

For the vector 
$$\vec{d}$$
,  $(d_i) = \frac{k_i(\vec{x}) - m_i}{k_i(\vec{x})}$   $i = 1, ..., I$ 

the uncertainty matrix for the set of benchmarks is

$$\overline{C}_{dd} = \overline{C}_{kk} + \overline{C}_{mm} - \overline{S}_k \overline{C}_{xm} - \overline{C}_{mx} \overline{S}_k^T$$
$$= \overline{S}_k \overline{C}_{xx} \overline{S}_k^T + \overline{C}_{mm} - \overline{S}_k \overline{C}_{xm} - \overline{C}_{mx} \overline{S}_k^T$$

GLLS involves minimizing this quantity:

$$Q(\vec{z},\vec{y}) = (\vec{y},\vec{z}) \cdot \begin{pmatrix} \bar{C}_{mm} & \bar{C}_{mx} \\ \bar{C}_{xm} & \bar{C}_{xx} \end{pmatrix}^{-1} \cdot (\vec{y},\vec{z})^{T},$$

subject to the constraint  $\vec{y} = \vec{d} + \vec{S}_k \vec{z}$ 

This is accomplished using Lagrange multipliers & minimizing this quantity:

$$R(\vec{z},\vec{y}) = Q(\vec{z},\vec{y}) + 2\lambda(\overline{S}_k\vec{z}-\vec{y})$$

 $\vec{z}$  and  $\vec{y}$  satisfy these relations:

$$\frac{\partial R(\vec{z},\vec{y})}{\partial \vec{z}} = \frac{\partial R(\vec{z},\vec{y})}{\partial \vec{y}} = 0$$

The results, giving the adjusted data & k's that minimize R are:

$$\Delta data: \qquad \vec{z} = \left( \vec{C}_{xm} - \vec{C}_{xx} \vec{S}_{k}^{T} \right) \cdot \vec{C}_{dd}^{-1} \cdot \vec{d}$$
  
$$\Delta k: \qquad \vec{y} = \left( \vec{C}_{mm} - \vec{C}_{mx} \vec{S}_{k}^{T} \right) \cdot \vec{C}_{dd}^{-1} \cdot \vec{d}$$

#### GLLS

GLLS gives the data adjustments (& resulting  $\Delta k$ 's) that minimize the Q or R functions (also called  $\chi^2$ )

The adjustments also give reduced uncertainties:

$$\bar{\boldsymbol{C}}_{m'm'} = \bar{\boldsymbol{C}}_{mm} - \left(\bar{\boldsymbol{C}}_{mm} - \bar{\boldsymbol{C}}_{mx}\bar{\boldsymbol{S}}_{k}^{T}\right) \cdot \bar{\boldsymbol{C}}_{dd}^{-1} \cdot \left(\bar{\boldsymbol{C}}_{mm} - \bar{\boldsymbol{S}}_{k}\bar{\boldsymbol{C}}_{xm}\right)$$

$$\bar{\boldsymbol{C}}_{\boldsymbol{x}\boldsymbol{x}\boldsymbol{x}^{\prime}} = \bar{\boldsymbol{C}}_{\boldsymbol{x}\boldsymbol{x}} - \left(\bar{\boldsymbol{C}}_{\boldsymbol{x}\boldsymbol{m}} - \bar{\boldsymbol{C}}_{\boldsymbol{x}\boldsymbol{x}}\bar{\boldsymbol{S}}_{\boldsymbol{k}}^{\mathsf{T}}\right) \cdot \bar{\boldsymbol{C}}_{\boldsymbol{d}\boldsymbol{d}}^{-1} \cdot \left(\bar{\boldsymbol{C}}_{\boldsymbol{m}\boldsymbol{x}} - \bar{\boldsymbol{S}}_{\boldsymbol{k}}\bar{\boldsymbol{C}}_{\boldsymbol{x}\boldsymbol{x}}\right)$$

The adjusted uncertainty matrix in k for a set of applications is:

$$\overline{C}_{k'k'} = \overline{S}_{k,A} \cdot \overline{C}_{x'x'} \cdot \overline{S}_{k,A}^{T}$$

where each row of  $\overline{S}_{k,A}$  is the sensitivity vector for an application. The square roots of diagonal elements in  $\overline{C}_{k'k'}$  are the relative  $1\sigma$  uncertainties in k for the adjusted data.

For a particular application i, the portion of MOS for nuclear data uncertainty is:

$$MOS_{data} = n_{\sigma} \cdot \sqrt{\left(\bar{C}_{k'k'}\right)}_{i,i}$$

where  $n_{\sigma}$  = 2 for 95% confidence, 2.6 for 99%

#### **Upper Subcritical Limit**

• To consider a simulated system subcritical, the computed keff must be less than the Upper Subcritical Limit (USL):

 $K_{calc} + 2\sigma_{calc} < USL$ 

USL = 1 + (Bias) - (Bias uncertainty) - MOS

MOS = MOS<sub>data</sub> + MOS<sub>code</sub> + MOS<sub>application</sub>

- The bias and bias uncertainty are at some confidence level, typically 95% or 99%.
  - These confidence intervals may be derived from a normal distribution, but the normality of the bias data must be justified.
  - Alternatively, the confidence intervals can be set using nonparametric methods.
LA-UR-17-27058 141

Whisper Usage

# **Using Whisper for Validation**

- As part of Whisper installation (not day-to-day use),
  - For each of the ~1100 benchmarks
    - MCNP6 is run to generate the sensitivity vector  $S_B$  for that benchmark
    - The sensitivity vector  $S_{\rm B}$  for each benchmark is saved in a folder
  - The nuclear data covariance files are saved in a folder
  - Benchmarks are checked for consistency, some may be rejected
  - Missing uncertainties for some benchmarks are estimated
  - All of this is the responsibility of the Admin person & needs to be done only once at installation (or repeated if the code, data, or computer change)
- To use Whisper for validation:
  - Use the whisper\_mcnp script to make 1 run with MCNP6 for a particular application, to generate the sensitivity vector for the application, S<sub>A</sub>
  - **②** Run Whisper, using the whisper\_usl script

# Whisper-1.1.0 – Batch Job

To try it, on Moonlight HPC front end, with Moab batch queueing system:

- Make a directory, copy MCNP6 input files to it
  - No blanks in pathname, directory name, input file names
  - Put mcnp6 input files in the directory

bash:	mkdir	WTEST	
bash:	ср	some-dir/myjob.i	WTEST

• Set up batch job file, job.txt

```
#!/bin/bash
#PBS -V
#PBS -l nodes=1:ppn=16,walltime=01:00:00
export WHISPER_PATH="/usr/projects/mcnp/ncs/WHISPER"
export PATH="$WHISPER_PATH/bin:$PATH"
cd WTEST
whisper_mcnp.pl -local myjob.i
whisper_usl.pl
```

• Submit batch job file

msub job.txt

# Whisper-1.1.0 – Interactive

### To try it, on Moonlight HPC:

- Set & export WHISPER\_PATH environment variable
  - bash:

export	WHISPER_PATH="/usr/projects/mcnp/ncs/WHISPER"
export	<b>PATH="\$WHISPER_PATH/bin:\$PATH"</b>

#### - csh, tcsh:

setenv	WHISPER_PATH	"/usr/projects/mcnp/ncs/WHISPER"
setenv	PATH	"\$WHISPER_PATH/bin:\$PATH"

- Make a directory, copy MCNP6 input files to it
  - No blanks in pathname, directory name, input file names
  - Put mcnp6 input files in the directory

bash:	mkdir	WTEST	
bash:	ср	some-dir/myjob.i	WTEST
bash:	ls	WTEST	
mjob.i			
bash:			

# Using whisper\_mcnp (1)

• From the front-end on an HPC system:

# whisper\_mcnp.pl myjob.i

- myjob.i is an MCNP6 input file
  - Must NOT include any of these cards: kopts, ksen, prdmp
  - May list more than 1 input file on whisper\_mcnp command line
  - Lots of options, see next 2 slides

### - Creates files & dirs:

MCNPInputList.toc	
Calcs/	
Calcs/myjob.i	← modified to include kopts, ksen, prdmp, & new kcode
KeffSenLib/	

### - Submits jobs to HPC compute nodes

- Single-node jobs, 16 threads each
- Default time limit of 1 hr

# Using whisper\_mcnp (2)

- For each MCNP6 input file listed on the whisper\_mcnp command line:
  - KCODE line is deleted & these lines are inserted:

```
kcode
                          100
                                 600
         100000
                   1.0
kopts blocksize = 5
ksen1 xs
     rxn = +2 + 4 - 6 + 16 102 103 104 105 106 107 - 7 - 1018
     erg = 1.0000e-11 \ 3.0000e-09 \ 7.5000e-09 \ 1.0000e-08 \ 2.5300e-08 \ 3.0000e-08
           4.0000e-08 5.0000e-08 7.0000e-08 1.0000e-07 1.5000e-07 2.0000e-07
           2.2500e-07 2.5000e-07 2.7500e-07 3.2500e-07 3.5000e-07 3.7500e-07
           4.0000e-07 6.2500e-07 1.0000e-06 1.7700e-06 3.0000e-06 4.7500e-06
           6.0000e-06 8.1000e-06 1.0000e-05 3.0000e-05 1.0000e-04 5.5000e-04
           3.0000e-03 1.7000e-02 2.5000e-02 1.0000e-01 4.0000e-01 9.0000e-01
           1.4000e+00 1.8500e+00 2.3540e+00 2.4790e+00 3.0000e+00 4.8000e+00
           6.4340e+00 8.1873e+00 2.0000e+01
prdmp j 9999999
```

- Note that there are large numbers of neutrons/cycle & cycles for the KCODE input. While it
  may be tempting to reduce these to get shorter runs, that is discouraged since it is
  important to achieve reasonable statistical uncertainties on the sensitivity profiles for a large
  number of reactions, isotopes, & energies.
- After using whisper\_mcnp, after the MCNP6 jobs complete:
  - The Calcs/ directory will contain these files

myjob.i	modified MCNP6 input file, with kcode, ksen, kopts, prdmp
myjob.i <mark>o</mark>	output file from MCNP6 jobs
myjob.i <mark>r</mark>	runtpe file
myjob.i <mark>s</mark>	srctp file

### whisper\_mcnp.pl - Usage (1)

#### whisper\_mcnp.pl [Options] Filelist

#### **Options:**

-help	print this information
-local	run MCNP jobs locally, on this computer [default]
-submit	submit batch MCNP jobs, using slurm or moab
-slurm	use Slurm command sbatch for submits [default]
-moab	use Moab command msub for submits
-walltime x	walltime limit for submitted batch jobs (eg, 01:00:00)
-threads x	number of threads for MCNP6
-cmd_before s	<pre>command(s) to execute before running mcnp (if -submit)</pre>
-cmd_after s	<pre>command(s) to execute after running mcnp (if -submit)</pre>

#### **KCODE card overrides:**

-neutrons x	number	of	neutro	ons/	cycle	e foi	C MCNP	6
-discard x	number	of	inacti	lve	cycle	es fo	or MCN	<b>P6</b>
-cycles x	total r	numb	er of	сус	les f	for 1	4CNP6	

#### System overrides, see note below:

-mcnp x	pathname for MCNP6 executable
-data x	pathname for MCNP6 data, DATAPATH
-xsdir x	pathname for MCNP6 xsdir file
-sdk	create tsunami-b SDK sensitivity files

#### Filelist:

Names of MCNP6 input files. The names should not contain blanks. The files must include a KCODE card (that will be replaced), & must not contain KSENn, KOPTS, or PRDMP cards (they will be supplied)

### whisper\_mcnp.pl - Usage (2)

#### whisper\_mcnp.pl [Options] Filelist

#### For normal usage:

*	set the standard	environment variables for MCNP & Whisper:
	DATAPATH	pathname for directory holding nuclear data & xsdir files
	PATH	include the pathname for directory holding MCNP executables
	WHISPER_PATH	pathname for the topmost WHISPER directory
	PATH	include \$WHISPER PATH/bin before the MCNP bin directory

\* Avoid using these Whisper command-line options, except for unusual, special cases: -mcnp, -data, -xsdir, -sdk

#### **Defaults:**

	<pre>-local [default]</pre>	-submit
-walltime		01:00:00
-threads	4	16
-neutrons	10000	100000
-discard	100	100
-cycles	600	600
-mcnp	mcnp6	mcnp6
-data		
-xsdir	/xsdir_mcnp6.?	<pre>/xsdir_mcnp6.?</pre>

# Using whisper\_mcnp (4)

#### • Use whisper\_mcnp.pl to run mcnp6 & get sensitivity profiles

bash:	Cd WTEST	
bash:	whisper_mcnp.pl -submit	myjob.i

#### Screen output:

```
Input File TOC
               = MCNPInputList.toc
Calculation directory
                       = Calcs
Sensitivity directory
                       = KeffSenLib
Neutrons/cycle
                       = 100000
Cycles to discard
                       = 100
Total Cycles to run
                       = 600
                       = /usr/projects/mcnp/mcnpexe -6
MCNP6 executable
                       = /usr/projects/mcnp/MCNP DATA/xsdir mcnp6.1
XSDIR file
                       = /usr/projects/mcnp/MCNP DATA
DATAPATH
Threads
                        = 16
Wall-clock time for job = 01:00:00
All jobs will be submitted using moab
... process mcnp input file: myjob.i
...modified mcnp input file: Calcs/myjob.i
... submit mcnp job to cluster using moab: myjob.i
```

Using whisper\_mcnp (5)

After running whisper\_mcnp in directory WTEST:

whisper\_mcnp.pl myjob.i

Use moab commands to check job status: showq –u username When the submitted job is complete:

Files created by whisper\_mcnp & mcnp6:

```
WTEST/

myjob.i ← original

MCNPInputlist.toc

Calcs/

myjob.i myjob.io myjob.ir myjob.is

KeffSenLib/
```

Using whisper\_usl (1)

 From the front-end or compute node on an HPC system, run Whisper using the whisper\_usl script:

> cd WTEST whisper\_usl.pl

- Can optionally include ExcludeFile.dat, list of benchmark files to exclude from Whisper calculations
- Runs Whisper for application(s) myjob.i (etc)
- For each input file listed in MCNPInputList.toc:
  - Extract sensitivity profiles from Calcs/myjob.io, place into directory KeffSenLib/
  - Create (or add to) file KeffSenList.toc
  - Run Whisper using the sensitivity profiles for the application (myjob.i) and the collection of Whisper benchmark sensitivity profiles
  - Output to screen & file Whisper.out

# Using whisper\_usl (2)

• After running whisper\_mcnp & whisper\_usl:

```
whisper_mcnp.pl myjob.i
..... [wait for submitted mcnp6 job to complete]
whisper_usl.pl
```

Files created by whisper\_mcnp, mcnp6, & whisper\_usl:

# whisper\_usl.pl (3)

```
bash: whisper usl.pl
******
*
  whisper usl
                        set up & run Whisper validation calculations
*
                 *
*
                 *
******
   ====> setup files for whisper
        ---> setup for problem myjob.i
                ...extract sensitivity profile data from: Calcs/myjob.io
                ...copy
                          sensitivity profile data to:
                                                          KeffSenLib/myjob.ik
                ...extract calc Keff & Kstd
                                                          Calcs/mvjob.io
                                              data from:
                ... KeffCalc= 0.96740 +- 0.00057, ANECF= 1.4904E+00 MeV, EALF= 1.2150E-01 MeV
   ====> run whisper
/Users/fbrown/CODES/WHISPER/WHISPER.git/bin/whisper -a KeffSenList.toc -ap KeffSenLib
whisper-1.1.0
                                 2016-02-02
                                              (Copyright 2016 LANL)
WHISPER PATH
                               = /Users/fbrown/CODES/WHISPER
 Benchmark TOC File
                               = /Users/fbrown/CODES/WHISPER/Benchmarks/TOC/BenchmarkTOC.dat
 Benchmark Sensitivity Path
                               = /Users/fbrown/CODES/WHISPER/Benchmarks/Sensitivities
 Benchmark Correlation File
                               =
 Benchmark Exclusion File
                               =
 Benchmark Rejection File
                               =
                               = /Users/fbrown/CODES/WHISPER/CovarianceData/BLO-44g
 Covariance Data Path
 Covariance Adjusted Data Path =
 Application TOC File
                               = KeffSenList.toc
 Application Sensitivity Path = KeffSenLib/
 User Options File
                               =
Output File
                               = Whisper.out
```

### whisper\_usl.pl (4)

```
. . . . . .
Reading benchmark data ...
Reading application data ...
Reading covariance data ...
Reading adjusted covariance data ...
Calculating application nuclear data uncertainties ...
Calculating upper subcritical limits ...
....case
              1
                 Ck= 0.41263
              4 Ck= 0.36554
                                  ← all Ck's printed in Whisper.out,
....case
                                     only a few printed to the screen
              3 Ck = 0.63497
....case
        . . . . . . . .
            246 Ck= 0.18901
....case
                                                               baseline
                                       calc
                                                   data unc
                                                                           k(calc)
   application
                                       margin
                                                   (1-sigma)
                                                               USL
                                                                           > USL
                                                   0.00120
   myjob.i
                                       0.01329
                                                               0.97860
                                                                          -0.00972
```

# Whisper.out (1)

whisper-1.1.0		2016-02-02	(Copyright	2016 LAN	L)		
WHISPER_PATH	=	/Users/fbrow	n/CODES/WHI	ISPER			
Benchmark TOC File	=	/Users/fbrown/	CODES/WHISPE	R/Benchmark	s/TOC/Benchr	narkTOC.dat	
Benchmark Sensitivity Path	=	/Users/fbrown/	CODES/WHISPE	R/Benchmark	s/Sensitivit	ies	
Benchmark Correlation File	=						
Benchmark Exclusion File	=						
Benchmark Rejection File	=						
Covariance Data Path	=	/Users/fbrow	n/CODES/WH1	SPER/Cova	rianceData	/BLO-44g	
Covariance Adjusted Data Path	=						
Application TOC File	=	KeffSenList.	toc				
Application Sensitivity Path	=	KeffSenLib/					
User Options File	=						
Output File	=	Whisper.out					
Reading benchmark data							
benchma	rk	k(bench)	unc	k(calc)	unc	bias	unc
myjob	.i	1.00000	0.01100	1.01174	0.00007	-0.01174	0.01100
•••••							
246 benchmarks read 0	he	anchmarks exc	luded				
240 Denemarks read, 0	50		ruucu.				
Reading application data							
	ä	application	k(calc)	unc			
		myjob.i	0.96802	0.000	52		
Peading covariance data							
Reading covariance data	100	11					
Reauting covariance udta for	TO	/					
Pooding adjusted government	~+·						
Reading adjusted covariance d	ati 101	1 •••					
Reading covariance data for	TOC	/⊥					

# Whisper.out (2)

Calculating application n application	ucle	ear data u	ncertain	ties adjusted	prior		
myjob.i				0.00209	0.01221		
Calculating upper subcri	tica	al limits					
				calc	data unc	baseline	k(calc)
application				margin	(1-sigma)	USL	> USL
myjob.i				0.01334	0.00209	0.97623	-0.00686
Benchmark population	=	48					
Population weight	=	28.56732			- For this apr	plication 48	benchmarks
Maximum similarity	=	0.96434			wore select	od as noutr	onically similar
_						for wolld of	official enclusio
Bias	=	0.00850			& sumcient	for valid st	atistical analysis
Bias uncertainty	=	0.00484					
Nuc Data uncert margi	n =	0.00209			Benchmark	rankings s	hown below
Software/method margin	n =	0.00500					
Non-coverage penalty	=	0.0000					
					K		
benchmark				ck	weight		
pu-met-fast-011-001.i				0.9643	1.0000		
pu-met-fast-044-002.i				0.9641	0.9958		
pu-met-fast-021-002.i				0.9618	0.9545		
pu-met-fast-003-103.i				0.9602	0.9252		
pu-met-fast-026-001.i				0.9594	0.9099		
pu-met-fast-025-001.i				0.9584	0.8912		
pu-met-fast-032-001.i				0.9572	0.8699		
pu-met-fast-016-001.i				0.9546	0.8221		
pu-met-fast-027-001.i				0.9546	0.8217		
pu-met-fast-012-001.i				0.9167	0.1283		
pu-met-fast-040-001.i				0.9166	0.1269		
pu-met-fast-045-003.i				0.9163	0.1209		
pu-met-fast-045-004.i				0.9147	0.0909		
pu-met-fast-002-001.i				0.9145	0.0874		

# **Conclusions & Discussion**

The sensitivity-uncertainty-based tools provided by MCNP/Whisper & SCALE/Tsunami are relatively new. They should be used with caution, and results should be critically reviewed.

One particular strength of the S/U-based tools is the selection of the most appropriate benchmarks to use for an application. The S/U-based tools provide quantitative, physics-based results for identifying which benchmarks are most similar to an application.

Another unique strength of the S/U-based tools is the use of GLLS methods to provide a quantitative, physics-based estimate of the MOS<sub>data</sub> due to nuclear data uncertainties. For applications where the traditional 2-5% MOS is too limiting, the S/U-based tools may provide quantitative evidence for a reduced MOS. Caution and judgment are required.

In the near-term, S/U-based methods provide powerful tools for supporting, complementing, and extending traditional validation methods. It is expected that the use of S/U-based tools will expand as more experience & knowledge is acquired.

# Best Practices for Monte Carlo Criticality Calculations

- Monte Carlo Criticality Calculations
  - Methodology & Concerns
  - Convergence
  - Bias
  - Statistics
- Best Practices
  - Discussion
  - Conclusions

# Methodology & Concerns



# Convergence

- Monte Carlo codes use <u>power iteration</u> to solve for  $K_{eff} \& \Psi$  for eigenvalue ٠ problems
- **Power iteration convergence is well-understood:** ٠

n = cycle number,  $k_0, u_0 - fundamental$ ,  $k_1, u_1 - 1st$  higher mode

$$\Psi^{(n)}(\vec{r}) = \vec{u}_0(\vec{r}) + a_1 \cdot \rho^n \cdot \vec{u}_1(\vec{r}) + \dots$$
  
$$k_{eff}^{(n)} = k_0 \cdot \left[1 - \rho^{n-1}(1-\rho) \cdot g_1 + \dots\right]$$

- First-harmonic source errors die out as
- First-harmonic K<sub>eff</sub> errors die out as

 $\rho^{n}$ ,  $\rho = k_{1} / k_{0} < 1$ ρ<sup>n-1</sup> (1- ρ)

- Source converges slower than K<sub>eff</sub>
- Most codes only provide tools for assessing K<sub>eff</sub> convergence. ٠
- → MCNP computes Shannon entropy of the fission source distribution, H<sub>src</sub>

# Bias in K<sub>eff</sub> & Tallies

- Power iteration is used for Monte Carlo K<sub>eff</sub> calculations
  - For one cycle (iteration):
    - M<sub>0</sub> neutrons start
    - $M_1$  neutrons produced,  $E[M_1] = K_{eff} \cdot M_0$
  - At end of each cycle, must renormalize by factor  $M_0 / M_1$
  - Dividing by stochastic quantity ( $M_1$ ) introduces bias in  $K_{eff}$  & tallies
- Bias in Keff, due to renormalization

Bias in 
$$K_{eff} \propto \frac{1}{M}$$
 M = neutrons / cycle

- Bias in Keff is negative, nonconservative for NCS
- Power & other tally distributions are also biased, produces "tilt"

1st generation 2nd generation

3rd generation

# **Bias in Statistics**

- MC eigenvalue calculations are solved by power iteration
  - Tallies for one generation are <u>spatially correlated</u> with tallies in successive generations
  - The correlation is positive
  - MCNP & other MC codes ignore this correlation, so computed statistics are <u>smaller</u> than the real statistics
  - Errors in statistics are small/negligible for K<sub>eff</sub>, may be significant for local tallies (eg, fission distribution)
  - Running more cycles or more neutrons/cycle does <u>not</u> reduce the underprediction bias in statistics
  - (True  $\sigma^2$ ) > (computed  $\sigma^2$ ), since correlations are <u>positive</u>

$$\frac{\text{True } \sigma_{\bar{x}}^2}{\text{Computed } \sigma_{\bar{x}}^2} = \frac{\sigma_{\bar{x}}^2}{\tilde{\sigma}_{\bar{x}}^2} \approx 1 + 2 \cdot \begin{pmatrix} \text{sum of lag-i correlation} \\ \text{coeff's between tallies} \end{pmatrix}$$

### **Best Practices – MC Crit Calcs - Summary**

- To avoid bias in K<sub>eff</sub> & tally distributions:
  - Use 10K or more neutrons/cycle (maybe 100K+ for large system)
  - Always check convergence of both K<sub>eff</sub> & H<sub>src</sub>
  - Discard sufficient initial cycles
- To help with convergence & coverage:
  - Take advantage of problem symmetry, if possible
  - Use good initial source guess, cover fissionable regions -points in each fissile region, or volume source for large systems
- Run at least a few 100 active cycles to allow codes to compute reliable statistics
- Statistics on tallies from codes are <u>underestimated</u>, often by 2-5x; possibly make multiple independent runs [note: statistics on k<sub>eff</sub> are OK, <u>not</u> underestimated]

# **Other Suggestions**

### For serious work, my work-flow includes the actions below:

- In MCNP input files, include a summary of { date, names, changes }
- Confirm that calculations used correct versions of code, data, scripts
- Always look at geometry with MCNP plotter
- Always check convergence plots for Keff & Hsrc
- Always check output file (not screen) for lost particles
- Check details if any unusual warnings appear
- Record for each run:
  - Name, date, computer, input/output file names
  - keff  $\pm \sigma$  (combined col/trk/abs only)
  - EALF, ANECF, % fast/intermed/thermal fissions
  - For solutions, H/Pu<sup>239</sup> or H/U<sup>235</sup>
  - Any issues?

If I'm in a hurry & skip some of the above, I usually end up paying big-time later on – having to repeat work to resolve errors or confusion

# References

# Previous discussion of details concerning bias, convergence, & statistics and "Best Practices" presented at

- 2008 PHYSOR Monte Carlo workshop
- 2009 M&C Monte Carlo workshop
- 2009 Paper at NCSD topical meeting (best paper award)
- 2010 PHYSOR Monte Carlo Workshop
- 2008 present MCNP Criticality Classes

#### Presentations available at mcnp.lanl.gov

#### **Monte Carlo Methods**

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G.E. Whitesides, "Difficulty in Computing the k-effective of the World," Trans. Am. Nucl. Soc., 14, No. 2, 680 (1971).

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**Forrest Brown** 

OECD-NEA-WPNCS Expert Group meeting

Advanced Monte Carlo Techniques

Paris, June 2017

# Investigation of Clustering in MCNP6 Monte Carlo Criticality Calculations

LA-UR-17-25009



Monte Carlo Methods, Codes, & Applications (XCP-3) X Computational Physics Division

# Introduction

- Monte Carlo
  - Simulate particle behavior
  - Tally event occurences to estimate physical results
  - Must have enough particles to cover phase space of the problem
- The undersampling problem
  - Not enough particles to cover phase space
  - All MC results are questionable, possibly wrong
  - How can you diagnose the <u>absence</u> of coverage ?
  - The cure: Run more particles in the simulation
  - Questions: How many? How do you know it's enough?
- Clustering
  - For criticality problems
    - Iterations using next-generation fission source
    - Convergence assessment depends on fission source coverage
  - In some problems, repeated iterations lead to clustering

# Sutton's Model Problem

#### Recent references

- T.M. Sutton & A. Mittal, "Neutron Clustering in Monte Carlo Iterated-Source Calculations", ANS MCD 2017, Jeju, S. Korea, April 16-20, 2017
- A. Zoia, E. Dumonteil, "Neutron clustering: spatial fluctuations in multiplying systems at the critical point", ANS MCD 2017, Jeju, S. Korea, April 16-20, 2017

### Model problem for clustering investigations

- Homogeneous box
- 400 x 400 x 400 cm<sup>3</sup>
- reflecting boundary conditions
- One-speed:  $\Sigma_T = 1.0$ ,  $\Sigma_S = 0.6$ ,  $\Sigma_C = 0.2$ ,  $\Sigma_F = 0.2$ ,  $\nu = 2.4$ ,  $f(\mu) = \frac{1}{2}$
- **Exact solution**: uniform distribution of fission sites throughout volume of box
  - Start with initial source guess = exact solution, uniform in volume
  - Shannon entropy for exact uniform source distribution:  $H_{exact} = log_2(N_s)$ , where N<sub>s</sub> is the number of grid-cells in Shannon entropy mesh
  - For a 10 x 10 x 10 Shannon entropy mesh,  $H_{exact} = \log_2(1000) = 9.966$
  - Can compare actual  $H_{src}$  for calculations that vary some of the problem parameters to  $H_{exact}$ , as an indicator of clustering in this model problem



# **Clustering vs Neutrons/cycle**

### 1000 neutrons/cycle



Cycle 1

Cycle 1000

Cycle 2000

Cycle 3000

Cycle 4000

# **Clustering and Shannon Entropy**

### • Shannon entropy vs cycle



# For this model problem (running 5000 cycles)

- Visual inspection of plots of fission source points
- MCNP determination of  $\mathrm{H}_{\mathrm{ave}}$  for the last half of the problem

 $H_{ave} < 0.7 H_{exact}$  $H_{ave} > 0.7 H_{exact}$  corresponds to **severe** clustering corresponds to **some or no** clustering

# Clustering and Shannon Entropy (more)

- Shannon entropy
  - $H = Sum p_k \log_2(p_k),$

note:  $0 \log_2(0) = 0$ 

- For  $N_s = m x m x m$  bins, and N neutrons
  - Uniform particle distribution:  $H_{max} = log_2(N_S)$
  - All neutrons at same point:  $H_{min} = 0$
- Fundamental assumption:

 $N >> N_s$ , enough neutrons to get reliable  $p_k$  tallies

- Clustering reduces the computed Shannon entropy
  - If N is small, coverage is not sufficient for reliable  $p_k$  tallies
  - If  $N \sim N_s$  or  $N < N_s$ ,  $H_{max} = \log_2(N)$ , wrong!
  - Simple example
    - 10 x 10 x 10 mesh,  $N_s = 1000$ , N = 1000 neutrons

1 neut/bin, uniform	H = 9.97	
2 neuts/bin, 0 in others	H = 8.97	500 clusters of 2
4 neuts/bin, 0 in others	H = 7.97	250 clusters of 4
8 neuts/bin, 0 in others	H = 6.97	125 clusters of 8
125 neuts/bin, 0 in others	H = 3.00	8 clusters of 125
250 neuts/bin, 0 in others	H = 2.00	4 clusters of 250
500 neuts/bin, 0 in others	H = 1.00	2 clusters of 500
1000 neuts/bin, 0 in others	H = 0.00	1 cluster of 1000

# A Real Problem - Pu-sol-therm-012 Case 13



keff cucle numbe

# Pu-sol-therm-012 Case 13

- Examine source points in fissile solution
- No clustering is evident, even with only 1,000 neutrons/cycle

### 1000 neutrons/cycle



# Model Problem, with pu-sol-therm-012-13 Solution

### Model problem for clustering investigations

- Homogeneous box
- 400 x 400 x 400 cm<sup>3</sup>
- reflecting boundary conditions
- Material: fissile solution from pu-sol-therm-012-13



- Note that the volume is ~56x larger than pu-sol-therm-012-13
- Vary the solution density, 0.01 0.25 atoms/cm<sup>3</sup>, nominal = 0.10 atoms/cm<sup>3</sup>
  - note that density variation ~ size variation (L)

Higher density Larger size	<b>→</b>	more clustering
Small neuts/cycle Smaller mfp		

**Clustering vs Density** 

# (1,000 neuts/cycle)


## A real Problem – Realistic PWR Detailed Model

## Nakagawa & Mori model of 2D PWR, realistic

- 50,952 fuel pins with cladding
- 4,825 water tubes for rods or detectors
- Each assembly:
  - Explicit fuel pins & rod channels
  - 17 x 17 lattice of pins in each assembly
  - Enrichments: 2.1%, 2.6%, 3.1%
- ENDF/B-VII.1 nuclear data
- Usually run with 100k neuts/cycle
- For 3D whole-core, reactor was chosen to be 100 cm high, with water above & below



2.1% enrichment
2.6% enrichment
3.1% enrichment

## **PWR2D – Clustering vs Neutrons/cycle**

 $\ell_{\rm F} = 19.1 \, {\rm cm}$  $f^{max} = 14\%$  $f_{\rm H} = 1\%$ 



#### 50 neutrons/cycle



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			1
			1
-			Η
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#### 100 neutrons/cycle



#### 500 neutrons/cycle

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		20		1		
	1		5	1	-	

#### 1,000 neutrons/cycle

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#### 10,000 neutrons/cycle



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**Cycle 3000** 

-	10					
		1	4			
	12		12		12	
			1			
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Cycle 4000

Whole-core, 100 cm axial,

with fuel in

324 x 324 x 100

**Usually run** 

with 100k

neuts/cycle

no clustering

in routine

calculations

 $\ell_{\rm F} = 19.1 \, {\rm cm}$  $f^{max} = 28\%$  $f_{\rm H} = 2\%$ 



 $\ell_{\rm F} = 19.1 \, {\rm cm}$  $f^{max} = 139\%$  $f_{\rm H} = 10\%$ 

 $\ell_{\rm F} = 19.1 \, {\rm cm}$  $f^{max} = 277\%$ 

 $f_{\rm H} = 18\%$ 





Cycle 1000

Cycle 2000

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## **Conclusions, Comments, Suggestions**

- For most practical problems, clustering is not a concern
  - Most problems today: 10k, 100k, or more neutrons/cycle
    - mcnp6.2 will issue warning message if < 10k neuts/cycle</li>
  - For large reactors, it is routine to run very large neuts/cycle, to get more efficient performance on parallel clusters
- For large solution tanks, clustering is a concern
  - NCS practioners should (but probably won't) run 100k or 1M neuts/cycle
  - There are some very, very large solution tanks (with very low Keff)
  - But fortunately, Keff result should be conservative, even with clustering
    - Very large solution tank with clustering will be similar to infinite medium problem, with relatively few neutrons leaking. Keff will be overestimated, which is conservative for crit-safety
- Very important to develop a diagnostic for clustering
- Cluster diagnostic for storage racks may be very different from large solution tanks (due to empty space, loose-coupling, etc.)

# Practical Examples for NCS Analysts





## **Examples using Whisper**

- Pu Pyrochemical Processing
  - Example 1: Typical computational model: ingot
  - Example 2: Geometry: Annular
  - Example 3: Material: Pu-NaCl
  - Example 4: Reflection: Ta
  - Example 5: Moderation: Oil
- U Metal Examples
  - Example 6: U billet with graphite/furnace insulation reflection
  - Example 7: U cylinder with Ta Reflection
- General Studies
  - Example 8: Revisiting a Practical Application of the Single-Parameter-Subcritical-Mass Limit for Plutonium Metal with Whisper
  - Example 9: Critical-mass curves and USL-mass curves comparison

Note for examples & demo:

To save time for class demos & running on a laptop, the full suite of 1101 Whisper Benchmarks is not used. Rather, a set of 246 benchmarks including sensitivity profiles from a LANL NCS traditional validation suite is used as the catalog. Parameters for running MCNP6 to get application sensitivity profiles use reduced values to save run time.

## **Upper Subcritical Limit (USL)**

- For an application:
  - A calculated  $K_{eff}$  < 1.0 is NOT sufficient to ensure subcriticality
  - Must conservatively account for
    - · Bias & uncertainties in the calculational method
    - Uncertainties in the physical model (eg, mass, isotopics, geometry, ...)



### **Pyrochemical Processing**

- Electrorefining is a batch plutonium metal purification process
  - Feed: impure plutonium metal ingot
  - Product: pure plutonium metal ring
  - Waste: salt, anode heel, crucible



- Purification media is an equimolar NaCl/KCl molten salt at 740°C
  - A small amount of plutonium chloride seed to charge the electrolyte with Pu(III).
- Liquid plutonium oxidizes at the anode (ingot) into the electrolyte
- Pu(III) ion in transported through the electrolyte to the cathode
- Reduced to metal dripping into the outer cup

## Example 1

# 4.5 kg Pu Ingot, varying H/D

## Example 1: 4.5 kg Pu Ingot, varying H/D (1)

- 4.5 kg Pu-239 right-circular cylinder
- Pu density = 19.86 g/cm<sup>3</sup>
- Reflected radially with 1 inch of water
- Reflected on the bottom with 1/4 inch steel
- Vary the height-to-diameter (H/D) over the range 0.5 – 3.0
  - Start with wval1.txt, input for H/D = 1
     mcnp6 i=wval1.txt
  - Copy wval1.txt to wval1p.txt, then insert directives for mcnp\_pstudy
    - Define list for HD:

c @@@ HD = 0.5 1.0 1.5 2.0 2.5 3.0

 For a given H/D, compute Pu radius, then other dimensions

```
V = (Pu mass)/(Pu density)V = H\pi R^{2} = (H/D) \cdot 2\pi R^{3}R = \left[ V/2\pi (H/D) \right]^{1/3}
```

Use parameters for dimensions & location of KSRC point





### Example 1: 4.5 kg Pu Ingot, varying H/D (2)

```
wval1: 4500 g Pu metal, H/D = 1
c reflected 1 inch water radially,
c 0.25 in steel bottom
С
 1 1 -19.860000
                              imp:n=1
                 -1
11 3 -1.0
                 +1 -11
                              imp:n=1
14 6 -7.92
                 -30
                              imp:n=1
15 0
                 +11 +30 -20
                              imp:n=1
20 0 +20
                              imp:n=0
                     0 0 6.607662 3.303831
 1
  rcc 0 0 0
11
   rcc
       0 0 0
                     0 0 6.607662 5.843831
20 rcc 0 0 -2.54
                     0 0 91.44
                                   91.44
    rcc 0 0 -0.635
                     0 0 0.635
                                   76.20
30
kcode 10000 1.0 50 250
 ksrc 0 0 3.303831
m1 94239.80c 1
      1001.80c 0.66667
                          8016.80c 0.33333
m3
mt3 lwtr.20t
     24050.80c 0.000757334
m6
     24052.80c 0.014604423
     24053.80c 0.001656024
     24054.80c 0.000412220
     26054.80c 0.003469592
     26056.80c 0.054465174
     26057.80c 0.001257838
     26058.80c 0.000167395
     25055.80c 0.00174
     28058.80c 0.005255537
     28060.80c 0.002024423
     28061.80c 0.000088000
     28062.80c 0.000280583
     28064.80c 0.000071456
prdmp 9e9 9e9 1 9e9
```

```
wvallp: 4500 g Pu metal, various H/D
c reflected 1 inch water radially,
c 0.25 in steel bottom
С
  V = H pi R^{**2} = (H/D) 2pi R^{**3}
С
    R = (V/(2pi H/D) * * 1/3)
С
С
c 000
       HD
              = 0.5 1.0 1.5 2.0 2.5 3.0
С
 000
       PI
              = 3.141592654
С
 666
       VOL PU = (4500. / 19.86)
С
 666
       R PU
              = ((VOL PU/(2*PI*HD))**(1/3))
С
c 000
       HPU
              = ( 2*R \overline{P}U*HD )
       R H20 = (R PU + 2.54)
c 000
       KSRC Z = (HPU * 0.5)
  666
С
С
 Pu cylinder:
С
                  = 4500 q
С
       mass
                  = 19.86 \, q/cc
С
       density
       volume
                  = VOL PU
С
С
       radius Pu
                  = R PU
       height Pu
С
                  = H PU
       H/D
                  = HD
С
с H2O
       outer radius = R H20
С
      1 -19.860000
  1
                      -1
                                   imp:n=1
 11
      3 -1.0
                      +1 -11
                                   imp:n=1
      6 -7.92
                      -30
 14
                                   imp:n=1
 15
                      +11 +30 -20
                                   imp:n=1
      0
                      +20
                                   imp:n=0
 20
      0
                          0 0 H PU
                                     R PU
          0 0 0
  1
     rcc
     rcc 0 0 0
                          0 0 H PU
                                     R H2O
 11
 20
     rcc 0 0 -2.540000
                          0 \ 0 \ 9\overline{1.44}
                                     91.44
     rcc 0 0 -0.635000 0 0 0.635
                                     76.20
 30
        10000 1.0 50 250
 kcode
        0. 0. KSRC Z
 ksrc
С
..... etc.
```

#### Example 1: 4.5 kg Pu Ingot, varying H/D (3)

• Parameter study using mcnp\_pstudy, whisper\_mcnp, & whisper\_usl:

#### mcnp\_pstudy.pl -i wval1p.txt -whisper

use mcnp\_pstudy to create inp files
 inp\_case001, inp\_case002, ... inp\_case\_006

#### whisper\_mcnp.pl inp\_case\*

use whisper\_mcnp to run mcnp6 for each case &
 produce k<sub>eff</sub> & sensitivity profile tallies
 items in green are for class demo, so that cases run quickly,
 & should not be used for serious work
 -neutrons 10000 -discard 50 -cycles 250 -threads 4

```
whisper_usl.pl
```

use whisper\_usl to run Whisper & determine USL for each case

## Example 1: 4.5 kg Pu Ingot, varying H/D (4)

wval1, H/D = 1 mcnp6 i=wval1.txt	wval1 mcn	o, varying H p_pstudy -	I/D i wval1p.txt	-setup -rui	n
	HD=0.5	case001 KEF	F 7.87229E	-01 KSIG	4.09191E-04
k = 0.92401 (41)	HD=1.0	case002 KEB	F 8.34430E	-01 KSIG	4.20175E-04
K = 0.03491(41)	HD = 1.5	case003 KEB	F 8.29652E	-01 KSIG	4.19130E-04
	HD=2.0	case004 KEB	F 8.11958E	-01 KSIG	4.18723E-04
	HD=2.5	case005 KEF	F 7.93676E	-01 KSIG	4.63720E-04
	HD=3.0	case006 KEF	F 7.73434E	-01 KSIG	4.19664E-04



### Example 1: 4.5 kg Pu Ingot, varying H/D (5)

#### **MCNP6-Whisper Results**

	calc	data unc	baseline	k(calc)	pu-met-fast-044-003.i pu-met-fast-044-004.i	0.9896 0.9894	0.7926 0.7867
application	margin	(1-sigma)	USL	> USL	pu-met-fast-044-002.i	0.9887	0.7646
ingot.txt_1_in	0.01441	0.00076	0.97862	-0.14366	pu-met-fast-029-001.i	0.9867	0.7006
Development a sur	.1				pu-met-fast-021-002.i	0.9865	0.6966
Benchmark popu	llation =	44			pu-met-fast-011-001.i	0.9848	0.6430
Population wei	ignt =	25.38028			pu-met-fast-030-001.i	0.9845	0.6328
Maximum simila	arity =	0.99621			pu-met-fast-031-001.i	0.9844	0.6284
<b>D</b> <sup>1</sup> a a	_	0 00050			pu-met-fast-042-004.i	0.9823	0.5620
Blas Dies unset sin		0.00858			- pu-met-fast-042-006.i	0.9820	0.5543
Bias uncertair	nty =	0.00583			pu-met-fast-021-001.i	0.9815	0.5387
Nuc Data uncer	rt margin =	0.00076			pu-met-fast-042-003.i	0.9813	0.5304
Software/metho	ba margin =	0.00500			pu-met-fast-042-007.i	0.9812	0.5301
Non-coverage p	penalty =	0.00000			- pu-met-fast-042-005.i	0.9809	0.5189
					pu-met-fast-042-009.i	0.9808	0.5153
honghmark		alı	wojah		pu-met-fast-042-008.i	0.9807	0.5119
Dencimark	36 001 <del>i</del>				pu-met-fast-042-010.i	0.9802	0.4971
pu-met-fast-03	30-001.1	0.9902	0.995		pu-met-fast-042-012.i	0.9802	0.4959
pu-met-fast-02	22-001.1	0.9956	0.905	2	pu-met-fast-042-011.i	0.9800	0.4908
pu-met-fast-02	24-001.1	0.9950	0.981	2	pu-met-fast-042-002.i	0.9799	0.4873
pu-met-fast-00	23_001 i	0.9940	0.931	י ד	pu-met-fast-042-015.i	0.9795	0.4759
pu-met-fast-02	29-001.1 39-001 i	0.9937	0.920		pu-met-fast-042-013.i	0.9794	0.4707
pu-met-fast-0	$000_{001}$	0.9952	0.900	4	pu-met-fast-042-014.i	0.9793	0.4690
nu_met_fast_04	44-005.i	0.9917	0.859	± 8	pu-met-fast-027-001.i	0.9752	0.3389
pu-met-fast-03	$35_{-001}$ i	0.9913	0 8440	9	pu-met-fast-042-001.i	0.9748	0.3267
pu-met-fast-02	$25_{-001}$ i	0.9913	0.811	7	pu-met-fast-044-001.i	0.9743	0.3134
pu-met-fast-02	$19_{-001}$ i	0.9902	0.797	, 5	pu-met-fast-018-001.i	0.9741	0.3057
pu-met-iust-ot	59-001.1	0.9090	0.757	0	mix-met-fast-007-022.i	0.9733	0.2819
					pu-met-fast-003-103.i	0.9714	0.2215
					mix-met-fast-007-023.i	0.9709	0.2041
					mix-met-fast-001-001.i	0.9675	0.0979

pu-met-fast-045-005.i

pu-met-fast-032-001.i

0.9668

0.9644

0.0777

0.0015

**Traditional Validation Results:** 

USL = 0.99 - MOS - AoA = 0.97 - AoA

## **Example 2**

# 4.5 kg Pu Annulus, varying H & R<sub>in</sub>

## Example 2: 4.5 kg Pu Annulus, varying H & R<sub>in</sub> (1)

 Establishing Subcriticality – ANSI/ANS-8.1 mass subcritical limits apply to a single piece having no concave surfaces.

-Does SPSL apply to a ring with concave surfaces?

Is annular cylinder validated geometry?

From a typical traditional validation report

How can this be established; what benchmarks include this geometry? Are these benchmarks similar to the ring?

discs, cuboid, annular

Benchmark	<sup>240</sup> Pu wt%	Form	Geometry	Moderator / Reflector	<b>H</b> / <sup>239</sup> <b>Pu</b>	Other Materials
pu-sol-therm-032-001	10.0	Pu(NO3)4	Annular	Water/Water	449.5	Steel
pu-sol-therm-032-002	10.0	Pu(NO3)4	Annular	Water/Water	488.2	Steel
pu-sol-therm-032-003	10.0	Pu(NO3)4	Annular	Water/Water	555.3	Steel
pu-sol-therm-032-004	10.0	Pu(NO3)4	Annular	Water/Water	622.5	Steel
pu-sol-therm-032-005	10.0	Pu(NO3)4	Annular	Water/Water	700.7	Steel
pu-sol-therm-032-006	10.0	Pu(NO3)4	Annular	Water/Water	800.5	Steel
pu-sol-therm-032-007	10.0	Pu(NO3)4	Annular	Water/Water	850.5	Steel
pu-sol-therm-032-008	10.0	Pu(NO3)4	Annular	Water/Water	949.6	Steel
pu-sol-therm-032-009	10.0	Pu(NO3)4	Annular	Water/Water	1021.5	Steel

		_		
Parameter	Area of Applicability	╽╽┝		
Fissile Material	<sup>239</sup> Pu	] ]]		
Fissile Material Form	Pu Metal, PuO <sub>2</sub> , and Pu(NO <sub>3</sub> ) <sub>4</sub>			
H/ <sup>239</sup> Pu	$0 \le H^{239}$ Pu $\le 2807$	╽╙		
Average Neutron Energy Causing Fission (MeV)	$0.003 \le ANECF \le 1.935$			
<sup>240</sup> Pu	0 to 42.9 wt% <sup>240</sup> Pu			
Moderating Materials	none, water, graphite, polystyrene			
Reflecting Materials	none, water, steel, oil, Plexiglas, polyethylene, graphite, W, Cu, U, Th, Al, Ni, Fe, Pb, Cd, Mo, Be, BeO			
Other Materials	concrete, PVC, Ga, B, Gd, Ta			
Geometry	cylinder array, cylinder, slab, sphere, hemisphere, stacked			

#### 5.3 Metallic units

The enrichment subcritical limit for uranium and the mass subcritical limits given in Table 3 apply to a single piece having no concave surfaces.

#### Table 3 – Single-parameter subcritical limits for metal units

Parameter	Subcritical limits for			
	<sup>233</sup> U [15]	<sup>235</sup> U [16]	<sup>239</sup> Pu [17]	
Mass of fissile nuclide (kg)	6.0	20.1	5.0	

## Example 2: 4.5 kg Pu Annulus, varying H & R<sub>in</sub> (2)

- 4.5 kg Pu-239 right-circular cylinder, hollow
- Pu density = 19.86 g/cm<sup>3</sup>
- Reflected radially with 1 inch of water
- Reflected on the bottom with 1/4 inch steel
- Set the height to be same as solid cylinder with height-to-diameter (H/D) = 1.0, 2.0, 3.0
- For given height, vary inner radius over 0<sup>+</sup> 2 cm
  - Start with wval2.txt input

mcnp6 i=wval2.txt

#### - Copy wval2.txt to wval2p.txt, then insert directives for mcnp\_pstudy

Define list for solid HD:

c @@@ HD = 1.0 2.0 3.0

- For a given H/D, compute Pu height
- Define list for inner radius RIN\_PU

c @@@ RIN\_PU = 0.001 0.5 1.0 2.0

Then other dimensions & source

Solid cylinder V = (Pu mass)/(Pu density)  $V = H\pi R^2 = (H/D) \cdot 2\pi R^3$   $H = \left[ 4V(H/D)^2/\pi \right]^{1/3}$ Hollow cylinder  $V = H\pi (R_{out}^2 - R_{in}^2)$  $R_{out} = \left[ R_{in}^2 + V/\pi H \right]^{1/2}$ 







LA-UR-17-27058 193

### Example 2: 4.5 kg Pu Annulus, varying H & R<sub>in</sub> (3)

```
wval2p: 4500 g Pu metal ring, various H & Rin
wval2: 4500 g Pu metal ring, fixed Rin
      3 -1.0
                     -1
  1
                                    imp:n=1
                                              С
                                              c 000
  2
      1 -19.860000
                     +1 -2
                                                            = 3.141592654
                                    imp:n=1
                                                     PI
      3 -1.0
                     +2 -11
                                              c 666
                                                     VOL PU = (4500. / 19.86)
 11
                                    imp:n=1
                                                     Pu mass
                                                                = 4500 q
      6 -7.92
                     -30
                                    imp:n=1
                                              С
 14
                                                     Pu density = 19.86 \text{ g/cc}
 15
                     +11 +30 -20
                                    imp:n=1
                                              С
      0
                                                     Pu volume = VOL PU
 20
      0
                     +20
                                    imp:n=0
                                              С
                                              С
  1 rcc 0 0 0
                                   0.100000
                                              c set height to match ingot with various H/D
                     0 0
                          6.608
                         6.608
                                              C @@@ HD
  2 rcc 0 0 0
                     0 0
                                                         = 1.0 2.0 3.0
                                   3.305259
                                              c @@@ HEIGHT = ( (4*VOL PU*(HD**2)/PI)**(1/3) )
 11 rcc 0 0 0
                     0 0
                         6.608
                                   5.845259
 20 rcc 0 0 -2.540 0 0 91.44
                                  91.44
                                              С
 30 \text{ rcc} 0 0 - 0.635
                     0 0 0.635
                                  76.20
                                              c for hollow cylinder:
                                                  use same height as for solid ingot
                                              С
                                                  set various inner radii
kcode 10000 1.0 50 250
                                              С
                                                  set Rout for given height, mass, Rin
sdef pos=0 0 0 rad=d1 axs=0 0 1 ext=d2
                                              С
                                                     RIN PU = .001 0.5 1.0 2.0
 sil 0.100 3.305259
                                              С
                                                000
                                                     ROUT PU=(sqrt(RIN PU**2+VOL PU/(PI*HEIGHT)))
                                              c @@@
     -21 1
 sp1
                                                     ROUT H2O = ( OUTER PU + 2.54 )
                                                666
 si2
     0.0 6.60800
                                              С
 sp2
                                              С
          1
     0
                                                    3 -1.0
     94239.80c 1
                                                                                  imp:n=1
                                                1
                                                                    -1
m1
                                                2
                                                    1 -19.860000
                                                                   +1 -2
                                                                                  imp:n=1
m3
     1001.80c 0.66667
                         8016.80c 0.33333
     lwtr.20t
                                               11
                                                    3 -1.0
                                                                    +2 - 11
                                                                                  imp:n=1
mt3
                                               14
                                                    6 -7.92
                                                                    -30
                                                                                  imp:n=1
     24050.80c 0.000757334
m6
                                               15
                                                    0
                                                                   +11 +30 -20
                                                                                  imp:n=1
     24052.80c 0.014604423
                                               20
                                                    0
                                                                   +20
     24053.80c 0.001656024
                                                                                  imp:n=0
     24054.80c 0.000412220
                                                                       0 0 HEIGHT
                                                                                    RIN PU
                                                1
                                                   rcc
                                                         0 0 0
     26054.80c 0.003469592
                                                2
                                                         0 0 0
                                                                          HEIGHT
                                                                                    ROUT PU
                                                   rcc
                                                                       0 0
     26056.80c 0.054465174
                                                                      0 0 HEIGHT
     26057.80c 0.001257838
                                               11
                                                   rcc
                                                         0 0 0
                                                                                    ROUT H2O
                                               20
                                                         0 \ 0 \ -2.540
                                                                       0 0 91.44
                                                                                    91.4\overline{4}
     26058.80c 0.000167395
                                                   rcc
                                               30
                                                         0 0 -0.635
                                                                       0 0 0.635
                                                                                    76.20
     25055.80c 0.00174
                                                   rcc
     28058.80c 0.005255537
                                              kcode 10000 1.0 50 250
     28060.80c 0.002024423
                                              sdef pos= 0. 0. 0.
                                                                    rad=d1 axs=0 0 1 ext=d2
     28061.80c 0.000088000
                                               sil RIN PU ROUT PU
     28062.80c 0.000280583
                                                    -21^{-1}
     28064.80c 0.000071456
                                               sp1
                                               si2 0 HEIGHT
prdmp 9e9 9e9 1 9e9
                                               sp2
                                                    0 1
                                              ..... etc.
```

#### Example 2: 4.5 kg Pu Annulus, varying H & R<sub>in</sub> (4)

Parameter study using mcnp\_pstudy, whisper\_mcnp, & whisper\_usl:

#### mcnp\_pstudy.pl -i wval2p.txt -whisper

use mcnp\_pstudy to create inp files
 inp\_case001, inp\_case002, ..., inp\_case\_012

#### whisper\_mcnp.pl inp\_case\*

use whisper\_mcnp to run mcnp6 for each case &
 produce k<sub>eff</sub> & sensitivity profile tallies
 items in green are for class demo, so that cases run quickly,
 & should not be used for serious work
 -neutrons 10000 -discard 50 -cycles 250 -threads 4

whisper\_usl.pl

use whisper\_usl to run Whisper & determine USL for each case

### Example 2: 4.5 kg Pu Annulus, varying H & R<sub>in</sub> (5)

	HD=1 Rin=.001	case001 KEFF	8.34752E-01	4.35668E-04
wval2	HD=2 Rin=.001	case002 KEFF	8.12612E-01	4.09516E-04
mcnp6_i=wval2.txt	HD=3 Rin=.001	case003 KEFF	7.72725E-01	3.82627E-04
	HD=1 Rin=0.5	case004 KEFF	8.20432E-01	4.01135E-04
k = 0.83413 (42)	HD=2 Rin=0.5	case005 KEFF	7.95375E-01	4.60388E-04
wval2n	HD=3 Rin=0.5	case006 KEFF	7.54174E-01	3.96580E-04
	HD=1 Rin=1.0	case007 KEFF	7.88497E-01	3.95026E-04
mcnp_pstudy -i wval2p.txt	HD=2 Rin=1.0	case008 KEFF	7.62394E-01	3.90299E-04
-setun -run	HD=3 Rin=1.0	case009 KEFF	7.20810E-01	4.27354E-04
ootup run	HD=1 Rin=2.0	case010 KEFF	7.21523E-01	4.02775E-04
	HD=2 Rin=2.0	case011 KEFF	6.97954E-01	4.88269E-04
	HD=3 Rin=2 O	Case 012 KEFE	6 64037E-01	4 88326E-04



**C**)

## Example 2: 4.5 kg Pu Annulus, varying H & R<sub>in</sub> (6)

#### **MCNP6-Whisper Results**

	calc	e data	unc baseline	k(calc)
application	margi	n (1-sig	gma) USL	> USL
ringhd2.txt_0.4_in	0.014	64 0.000	0.97840	-0.17760
Benchmark population	n =	41		
Population weight	=	25.47164		
Maximum similarity	=	0.99532		
Bias	=	0.00836		
Bias uncertainty	=	0.00628		
Nuc Data uncert marc	in =	0.00075		
Software/method marc	, jin =	0.00500		
Non-coverage penalty	, =	0.0000		
benchmark		ck	weight	
pu-met-fast-036-001.	i	0.9953	1.0000	
pu-met-fast-024-001.	i	0.9941	0.9608	
pu-met-fast-044-005.	i	0.9933	0.9360	
pu-met-fast-011-001.	i	0.9928	0.9196	
pu-met-fast-044-004.	i	0.9925	0.9117	
pu-met-fast-044-003.	i	0.9898	0.8275	
$\overline{pu}$ -met-fast-023-001.	i	0.9890	0.8020	
 pu-met-fast-022-001.	i	0.9886	0.7898	
pu-met-fast-039-001.	i	0.9884	0.7823	

Benchmarks are the same as those for the ingot in example 1

#### **Traditional Validation Results:**

USL = 0.99 - MOS - AoA = 0.97 - AoA

benchmark	ck	weight
pu-met-fast-044-002.i	0.9876	0.7587
pu-met-fast-031-001.i	0.9875	0.7561
pu-met-fast-021-002.i	0.9867	0.7284
pu-met-fast-042-002.i	0.9863	0.7158
pu-met-fast-042-004.i	0.9862	0.7124
pu-met-fast-042-003.i	0.9861	0.7104
pu-met-fast-001-001.i	0.9859	0.7051
mix-met-fast-009-001.i	0.9854	0.6873
pu-met-fast-035-001.i	0.9851	0.6798
pu-met-fast-009-001.i	0.9846	0.6633
pu-met-fast-042-006.i	0.9843	0.6536
pu-met-fast-042-005.i	0.9840	0.6446
pu-met-fast-042-007.i	0.9833	0.6237
pu-met-fast-042-001.i	0.9833	0.6230
pu-met-fast-025-001.i	0.9829	0.6103
pu-met-fast-042-008.i	0.9825	0.5980
pu-met-fast-027-001.i	0.9825	0.5975
pu-met-fast-042-009.i	0.9821	0.5843
pu-met-fast-042-010.i	0.9815	0.5667
pu-met-fast-042-011.i	0.9811	0.5543
pu-met-fast-042-012.i	0.9808	0.5435
pu-met-fast-042-013.i	0.9800	0.5202
pu-met-fast-042-014.i	0.9799	0.5175
pu-met-fast-042-015.i	0.9799	0.5159
pu-met-fast-030-001.i	0.9782	0.4626
pu-met-fast-021-001.i	0.9780	0.4560
pu-met-fast-029-001.i	0.9777	0.4468
pu-met-fast-044-001.i	0.9743	0.3409
pu-met-fast-018-001.i	0.9720	0.2678
	0.9690	0.1754
mix-met-fast-007-023.i	0.9655	0.0635
pu-met-fast-045-005.i	0.9653	0.0586

## **Example 3**

## 4.5 kg Pu-NaCl Mixture

## Example 3: 4.5 kg Pu-NaCl Mixture (1)

- 4.5 kg Pu (0) sphere mixed with variable amounts (0-2 kg) of NaCl
- Reflected with 1 inch of water
- Density of Pu = 19.86 g/cm<sup>3</sup>
- Density of NaCl = 1.556 g/cm<sup>3</sup>



Run commands:

mcnp\_pstudy -i wval3p.txt -whisper whisper\_mcnp.pl inp\_case\* whisper\_usl.pl

For whisper\_mcnp.pl, these (nondefault) options are used for class: -neutrons 10000 -discard 50 -cycles 250 -threads 4

#### Example 3: 4.5 kg Pu-NaCl Mixture (2)

С

С

```
Study of Pu mixed with NaCl
wval3:
 1
     4 - 6.163863
                           imp:n=1
                    -1
                    +1 -2 imp:n=1
 2
     1 -1.0
                                              С
20
                    +2
     0
                           imp:n=0
                                              С
                                              С
                                              С
 1 sph 0 0 0
                 5.98941813698262
                                              С
 2 sph 0 0 0
                 8.52941813698262
                                              С
kcode 10000 1.0 150 500
sdef pos=0 0 0
                  rad=d1
      0 5.989
 si1
                                              С
 sp1
      -21 2
                                              С
      1001.80c 2
                      8016.80c 1
m1
mt1
      lwtr.20t
m4
      94239.80c -0.81117881
      11023.80c - 0.07427730
                                              С
                                              С
      17035.80c -0.08561650
      17037.80c -0.02893221
                                              С
                                               1
                                               2
                                              20
                                               1
                                               2
```

```
wval3p: Pu mixed with NaCl
c 000
             PI = 3.141592654
c @@@ PU MASS = 4500
C @@@ PU VOL
               = ( PU MASS / 19.86 )
c @@@ NACL MASS = 1.e-6 500 1000 1500 2000
c @@@ NACL VOL = (NACL MASS / 1.556)
   Pu
        mass = PU MASS g
   NaCl mass = NACL MASS g
  Pu density (pure) = 19.86 g/cc
   NaCl density (pure) = 1.556 g/cc
                 = ( PU VOL + NACL VOL
c @@@ VOLUME
                 = ( PU MASS + NACL MASS )
c @@@ MASS
C @@@ DENSITY
                 = ( -MASS/VOLUME )
c @@@ DENSITY PU = (PU MASS/VOLUME)
      Pu density = DENSITY PU q/cc
c @@@ RADIUS
                 = ((0.75 \times VOLUME/PI) \times (1/3))
c @@@ OUTER H2O
                 = ( RADIUS + 2.54 )
c @@@ A11023 = 22.98976928
c @@@ A17035 = ( 34.96885268 * 0.7576 )
c @@@ A17037 = ( 36.96590259 * 0.2424 )
c @@@ A NACL = (A11023 + A17035 + A17037)
 @@@ MF94239 = ( -PU MASS/MASS )
c @@@ MF11023 = ( -NACL MASS*(A11023/A NACL)/MASS )
c @@@ MF17035 = ( -NACL MASS*(A17035/A NACL)/MASS )
c @@@ MF17037 = ( -NACL MASS*(A17037/A NACL)/MASS )
                         imp:n=1
     4 DENSITY
                   -1
    1 -1.0
                  +1 -2 imp:n=1
     0
                  +2
                         imp:n=0
        RADIUS
    SO
        OUTER_H2O
    SO
kcode 10000 1.0 50 250
sdef pos=0 0 0 rad=d1
sil O RADIUS
 sp1
     -21 2
      1001.80c 2
                     8016.80c 1
m1
      lwtr.20t
mt1
m4
      94239.80c MF94239
      11023.80c MF11023
      17035.80c MF17035
      17037.80c MF17037
prdmp 9e9 9e9 1 9e9
```

### Example 3: 4.5 kg Pu-NaCl Mixture (3)

#### **MCNP6-Whisper Results**



### Example 3: 4.5 kg Pu-NaCl Mixture (4)

#### **MCNP6-Whisper Results**

		USL baseline = .979
Benchmark population	=	46
Benchmark weight	=	25.75745
Benchmark similarity	=	0.99245
Bias	=	0.00796
Bias uncertainty	=	0.00682
Nuc Data	=	0.0012
Software/method margin	=	0.005
Non-coverage penalty	=	0

benchmark	ck	weight	
pu-met-fast	-011-001.i	0.9924	1
pu-met-fast	-044-004.i	0.9842	0.8636
pu-met-fast	-042-001.i	0.9831	0.8448
pu-met-fast	-042-002.i	0.9828	0.8396
pu-met-fast	-044-005.i	0.9827	0.8377
pu-met-fast	-027-001.i	0.981	0.8107
pu-met-fast	-036-001.i	0.9805	0.8018
pu-met-fast	-042-003.i	0.9802	0.7965
pu-met-fast	-031-001.i	0.9792	0.7798
pu-met-fast	-042-004.i	0.9787	0.7727
pu-met-fast	-024-001.i	0.978	0.7604
pu-met-fast	-044-003.i	0.9768	0.7401
pu-met-fast	-042-005.i	0.9757	0.7213
pu-met-fast	-042-006.i	0.9746	0.7039
pu-met-fast	-021-002.i	0.9737	0.6893

#### **Traditional Validation Results:**

USL = 0.99 - MOS - AoA = 0.97 - AoA

pu-met-fast-044-002.i	0.9734	0.6832
pu-met-fast-042-007.i	0.9734	0.6832
pu-met-fast-042-008.i	0.9722	0.6645
pu-met-fast-042-009.i	0.9709	0.6426
pu-met-fast-042-010.i	0.9705	0.6356
pu-met-fast-042-011.i	0.9699	0.6257
pu-met-fast-023-001.i	0.9691	0.6133
pu-met-fast-042-012.i	0.9687	0.6054
pu-met-fast-039-001.i	0.9683	0.5993
pu-met-fast-042-014.i	0.9681	0.5961
pu-met-fast-042-013.i	0.9681	0.5959
pu-met-fast-042-015.i	0.9676	0.587
pu-met-fast-022-001.i	0.9644	0.534
pu-met-fast-009-001.i	0.964	0.5284
pu-met-fast-035-001.i	0.9629	0.5093
mix-met-fast-009-001.i	0.9618	0.4919
pu-met-fast-044-001.i	0.9612	0.482
pu-met-fast-001-001.i	0.9602	0.4653
pu-met-fast-025-001.i	0.9593	0.4499
pu-met-fast-021-001.i	0.9588	0.4424
pu-met-fast-030-001.i	0.9559	0.3941
pu-met-fast-018-001.i	0.9555	0.3863
pu-met-fast-029-001.i	0.951	0.3115
pu-met-fast-045-005.i	0.9509	0.3097
mix-met-fast-007-022.i	0.9496	0.2897
mix-met-fast-007-023.i	0.9448	0.2093
pu-met-fast-019-001.i	0.9421	0.1637
pu-met-fast-038-001.i	0.9384	0.1032
mix-met-fast-001-001.i	0.9374	0.0871
pu-met-fast-040-001.i	0.9355	0.055
pu-met-fast-003-103.i	0.9352	0.0505

\*bold indicates same benchmark selected for Pu ingot

## **Example 4**

# 4.5 kg Pu Sphere, Ta Reflector, various thicknesses

#### **Example 4: Ta-reflected Pu**

#### Reflection: Ta

From a typical traditional validation report

- Is Ta validated as a reflector in the AoA?
- What can be done to answer this question and, if needed, possibly extend AoA?

Parameter	Area of Applicability
Fissile Material	<sup>239</sup> Pu
Fissile Material Form	Pu Metal, PuO <sub>2</sub> , and Pu(NO <sub>3</sub> ) <sub>4</sub>
H/ <sup>239</sup> Pu	$0 \le H^{239}$ Pu $\le 2807$
Average Neutron Energy Causing Fission (MeV)	$0.003 \le ANECF \le 1.935$
<sup>240</sup> Pu	0 to 42.9 wt% <sup>240</sup> Pu
Moderating Materials	none, water, graphite, polystyrene
Reflecting Materials	none, water, steel, oil, Plexiglas, polyethylene, graphite, W, Cu, U, Th, Al, Ni, Fe, Pb, Cd, Mo, Be, BeO
Other Materials	concrete, PVC, Ga, B, Gd, Ta
Geometry	cylinder array, cylinder, slab, sphere, hemisphere, stacked discs, cuboid, annular

#### • CSSG Response on Validation with Limited Benchmark Data:

"For those situations where a nuclide is determined to be important and limited data exist, validation may still be possible. However, an additional margin should be used to compensate for the limited data. This margin is separate from, and in addition to, any margin needed for extending the benchmark applicability to the validation. Sensitivity and uncertainty tools may be used as part of the technical basis for determining the magnitude of the margin."

## Example 4: 4.5 kg Pu Sphere, Ta-reflected (1)

- 4.5 kg Pu-239 sphere
- Pu density = 19.8 g/cm<sup>3</sup>
- Reflected radially with Ta
- Vary the Ta-reflector thickness over the range 0.<sup>+</sup> – 30. cm



- Start with wval4.txt, input for thickness=7.62
   mcnp6 i=wval4.txt
- Copy wval4.txt to wval4p.txt, then insert directives for mcnp\_pstudy
  - Define list for thickness:
    - c @@@ THICK = 0.01 5. 10. 15. 20. 25. 30.
  - For a given THICK, compute reflector Rin & Rout
  - Use parameters for dimensions & location of KSRC point
  - Run:

mcnp\_pstudy.pl -i wval4p.txt -whisper whisper\_mcnp.pl inp\_case\* whisper\_usl.pl

### Example 4: 4.5 kg Pu Sphere, Ta-reflected (2)

```
wval4: Study of Pu reflected with Ta
                                                 wval4p: Study of Pu reflected with Ta
С
                                                 С
              = 4500 q
                                                                = 4500 q
С
  Pu mass
                                                 С
                                                   Pu mass
   Pu density = 19.8 \text{ g/cc}
                                                   Pu density = 19.8 \text{ q/cc}
С
                                                 С
   Pu volume = 227.272727
                                                    Pu volume = 227.272727
                                                 С
С
С
                                                 С
  reflector definition:
                                                    vary reflector thickness from 0+ to 30 cm
С
                                                 С
С
     reflector thickness
                             = 7.62
                                                 С
                                                    000
                                                                  = .01 5. 10. 15. 20. 25. 30.
     reflector inner radius = 3.7857584
                                                        THICK
                                                 С
С
     reflector outer radius = 11.405758
                                                    @@@ R INNER = 3.7857584
С
                                                 С
                                                     000
                                                         R OUTER = ( R INNER + THICK )
С
                                                 С
      4 -19.80 -1
                           imp:n=1
  1
                                                 С
      1 - 16.69 + 1 - 2
                           imp:n=1
                                                   reflector definition:
  2
                                                 С
                                                       reflector thickness
                           imp:n=0
 20
      0
                +2
                                                 С
                                                                               = THICK Cm
                                                       reflector inner radius = R INNER cm
                                                 С
                                                       reflector outer radius = R OUTER cm
  1 so 3.7857584
                                                 С
        11.405758
  2 so
                                                  С
                                                        4 -19.80 -1
                                                                             imp:n=1
                                                   1
 kcode 10000 1.0 50 250
                                                        1 - 16.69 + 1 - 2
                                                                             imp:n=1
                                                    2
 sdef pos=0 0 0 rad=d1
                                                                             imp:n=0
                                                   20
                                                        0
                                                                  +2
  si1 0 3.78
  sp1 -21 2
                                                            R INNER
                                                    1 so
                                                   2 so
                                                            R OUTER
С
                          73181.80c 0.99988
 m1 73180.80c 0.00012
                                                  kcode 10000 1.0 50 250
 m4 94239.80c 1
                                                   sdef pos=0 0 0 rad=d1
 prdmp 9e9 9e9 1 9e9
                                                   sil O R INNER
                                                   sp1 -21 2
                                                 С
                                                  m1 73180.80c 0.00012
                                                                           73181.80c 0.99988
                                                       94239.80c 1
                                                  m4
                                                  prdmp 9e9 9e9 1 9e9
```

### Example 4: 4.5 kg Pu Sphere, Ta-reflected (3)

wval4, thick=7.62 mcnp6 i=wval4.txt	wval4p, varying thick mcnp_pstudy -i wval4p.txt -setup -run				
	T=.01 case001 KEFF 7.91693E-01 KSIG 3.14948E	-04			
	T=5.0 case002 KEFF 9.27157E-01 KSIG 4.47334E	-04			
k = 0.94638 (41)	T=10. case003 KEFF 9.54775E-01 KSIG 4.11031E	-04			
	T=15. case004 KEFF 9.61644E-01 KSIG 4.34033E	-04			
	T=20. case005 KEFF 9.62867E-01 KSIG 4.37235E	-04			
	T=25, case006 KEFF 9.63899E-01 KSIG 4.04508E	-04			
	T-30 C250007 KEEE 9 63160E-01 KSIG / 27633E	_0/			



#### LA-UR-17-27058 208

### **Example 4: Ta-reflected Pu**

#### **MCNP6 and Whisper Results**

	calc	data unc	baseline	k(calc)
application	margin	(1-sigma)	USL	> USL
tarefl.txt_7.62_in	0.01707	0.01502	0.93889	0.00750

Benchmark population	=	119		
Population weight	=	60.92464		
Maximum similarity	=	0.64075	r	Trouble ! Benchmarks are
Bias	=	0.00912		not verv similar
Bias uncertainty	=	0.00795		to application
Nuc Data uncert margin	=	0.01502	<b>~</b>	
Software/method margin	=	0.00500		
Non-coverage penalty	=	0.00000		
benchmark			ck 🖌	weight
pu-met-fast-045-00	5.i		0.6408	1.0000
pu-met-fast-045-004	4.i		0.6400	0.9986
pu-met-fast-045-003	3.i		0.6368	0.9926
pu-met-fast-045-002	2.i		0.6297	0.9796
pu-met-fast-045-00	7.i		0.6259	0.9725
pu-met-fast-045-00	l.i		0.6213	0.9641
pu-met-fast-045-00	5.i		0.5469	0.8270
pu-met-fast-023-00	l.i		0.4203	0.5937
pu-met-fast-039-00	1.i		0.4201	0.5935

#### **Traditional Validation Results:**

USL = 0.99 - MOS - AoA = 0.97 - AoA

#### Run using all 1101 Whisper benchmarks, not just 246 benchmarks for class

benchmark	ck	weight
mix-met-fast-009-001.i	0.4193	0.5919
pu-met-fast-009-001.i	0.4190	0.5914
pu-met-fast-035-001.i	0.4189	0.5913
pu-met-fast-022-001.i	0.4185	0.5904
pu-met-fast-025-001.i	0.4183	0.5900
pu-met-fast-036-001.i	0.4180	0.5896
pu-met-fast-001-001.i	0.4180	0.5895
pu-met-fast-021-002.i	0.4176	0.5887
pu-met-fast-030-001.i	0.4171	0.5879
pu-met-fast-024-001.i	0.4171	0.5878
pu-met-fast-021-001.i	0.4165	0.5867
pu-met-fast-044-003.i	0.4164	0.5866
pu-met-fast-044-005.i	0.4162	0.5863
pu-met-fast-044-002.i	0.4160	0.5858
pu-met-fast-029-001.i	0.4155	0.5850
pu-met-fast-044-004.i	0.4146	0.5832
pu-met-fast-003-103.i	0.4141	0.5823
pu-met-fast-042-015.i	0.4134	0.5811
pu-met-fast-042-012.i	0.4134	0.5811
mix-met-fast-007-022.i	0.4134	0.5811
pu-met-fast-042-011.i	0.4134	0.5810
pu-met-fast-042-009.i	0.4134	0.5810
pu-met-fast-042-013.i	0.4133	0.5808
pu-met-fast-042-014.i	0.4133	0.5808
pu-met-fast-042-010.i	0.4133	0.5808
pu-met-fast-042-007.i	0.4132	0.5807
pu-met-fast-018-001.i	0.4132	0.5806
pu-met-fast-042-006.i	0.4131	0.5806
pu-met-fast-042-008.i	0.4131	0.5805

• • • •

### **Example 4: Ta-reflected Pu**

- None of the benchmarks appear to have the same neutronics as the application
  - Largest C<sub>k</sub> in the Whisper example output is 0.64 very low
  - Guidance from ORNL Scale/Tsunami developers:

0.95 < C <sub>k</sub>	$\rightarrow$	great
$0.90 < C_k < 0.95$	$\rightarrow$	good
C <sub>k</sub> < 0.90	$\rightarrow$	not so good

- If all C<sub>k</sub>'s are low, there is a need to expand the benchmark suite, add similar benchmarks
- If no similar benchmarks, need extra analysis, analyst judgment, & margin



 Need to find more benchmarks with Ta reflector & add to Whisper suite, if Ta-reflected applications are expected



## **Example 5**

# 4.5 kg Pu Sphere, Oil moderated

### **Example 5: Oil-Moderated Pu**

- Is Pu moderated with oil included in validation AoA?
  - If not, what can be done?

Parameter	Area of Applicability
Fissile Material	<sup>239</sup> Pu
Fissile Material Form	Pu Metal, PuO <sub>2</sub> , and Pu(NO <sub>3</sub> ) <sub>4</sub>
H/ <sup>239</sup> Pu	$0 \le H^{239}$ Pu $\le 2807$
Average Neutron Energy Causing Fission (MeV)	$0.003 \le \text{ANECF} \le 1.935$
<sup>240</sup> Pu	0 to 42.9 wt% <sup>240</sup> Pu
Moderating Materials	none, water, graphite, polystyrene
Reflecting Materials	none, water, steel, oil, Plexiglas, polyethylene, graphite, W, Cu, U, Th, Al, Ni, Fe, Pb, Cd, Mo, Be, BeO
Other Materials	concrete, PVC, Ga, B, Gd, Ta
Geometry	cylinder array, cylinder, slab, sphere, hemisphere, stacked discs, cuboid, annular

- Does the calculation model fit within the area of applicability of the benchmark critical experiments used for the code validation?
- For systems which are outside the validation applicability, an AoA margin may be warranted, depending on the specific problem being analyzed.
- The resulting USL with an AoA margin is defined as

USL = 1.0 + (bias) – (bias uncertainty) – (margin of subcriticality) – (AoA margin)



#### LA-UR-17-27058 212

## Example 5: Oil-Moderated Pu

- MCNP6 Input
- 4.5 kg Pu (0) sphere mixed with variable amounts of Hydraulic oil
- Pu concentration range: -19.8 g Pu/cm<sup>3</sup>
- Hydraulic oil composition: C<sub>40</sub>H<sub>33</sub>O<sub>4</sub>Cl<sub>6</sub>P
- Hydraulic oil density:
   0.871 g/cm<sup>3</sup>
- Reflected with 1 inch of water

```
Pu mixed with hydraulic oil
С
1
    4 - 1.827099
                          imp:n=1
                  -1
2
    1 -1.0
                  +1 -2
                         imp:n=1
20
                  +2
                          imp:n=0
    0
         10.2417609488294
1
   SO
2
   SO
         12.7817609488294
kcode 10000 1.0 150 500
ksrc 0 0 0
С
     1001.80c 2
m1
     8016.80c 1
    lwtr.20t
mt1
     94239.80c
                -0.54731523
m4
      1001.80c
                -0.01821054722413
      6000.80c -0.264852020155431
      8016.80c -0.0352799376428247
     15031.80c
                -0.0170753227802324
     17035.80c
                -0.0876520545992508
     17037.80c
                -0.0296143373586584
```
### **Example 5: Oil-Moderated Pu**

### MCNP6 and Whisper Results



### **Example 5: Oil-Moderated Pu**

### **MCNP6 and Whisper Results**

	calc	data unc	baseline	k(calc)			
application	margin	(1-sigma)	USL	> USL			
<pre>puoilmix.txt_7_in</pre>	0.01477	0.00109	0.97739	-0.41445			
Benchmark popul	ation =	65				0 0200	0 7500
Population weig	jht =	28.56693			pu-comp-mixed-002-001.1	0.9388	0.7502
Maximum similar	ity =	0.96433			pu-met-fast-042-005.1	0.93/3	0./353
					pu-comp-mixed-002-002.1	0.9344	0.7077
Bias	=	0.00720			pu-met-fast-042-006.1	0.9344	0.7069
Bias uncertaint	- y =	0.00757			pu-met-fast-042-007.1	0.9320	0.6840
Nuc Data uncert	. margin =	0.00109			pu-met-fast-036-001.1	0.9310	0.6/36
Software/method	l margin =	0.00500			pu-met-fast-044-003.1	0.9307	0.6714
Non-coverage pe	enalty =	0.0000			pu-met-fast-042-008.1	0.9303	0.6673
	-				pu-met-fast-024-001.1	0.9277	0.6417
benchmark		ck	weight		pu-met-fast-042-009.1	0.92/1	0.6360
pu-met-fast-042	2-001.i	0.9643	1.0000		pu-met-fast-042-010.1	0.9268	0.6327
- pu-met-fast-011	-001.i	0.9641	0.9973		pu-comp-mixed-002-003.1	0.9267	0.6315
- pu-met-fast-027	-001.i	0.9580	0.9377		pu-met-fast-042-011.1	0.9255	0.6198
pu-met-fast-042	2-002.i	0.9561	0.9199		pu-met-fast-042-012.1	0.9228	0.5943
- pu-met-fast-042	2-003.i	0.9483	0.8436		pu-met-fast-044-002.1	0.9224	0.5899
- pu-met-fast-044	-004.i	0.9474	0.8343		pu-met-fast-042-014.1	0.9224	0.5896
pu-met-fast-042	2-004.i	0.9444	0.8048		pu-met-fast-042-013.i	0.9222	0.5881
pu-met-fast-031	-001.i	0.9425	0.7861		pu-met-fast-042-015.1	0.9209	0.5752
pu-met-fast-044	-005.i	0.9404	0.7658		pu-comp-mixed-002-004.i	0.9191	0.5574
-					pu-met-fast-021-002.i	0.9184	0.5506
					pu-met-fast-044-001.i	0.9145	0.5128
					pu-met-fast-023-001.i	0.9046	0.4156
					pu-met-fast-039-001.i	0.9031	0.4015
					pu-comp-mixed-002-005.i	0.9030	0.3999
					pu-met-fast-018-001.i	0.9008	0.3782
					pu-met-fast-021-001.i	0.8989	0.3598
					pu-met-fast-009-001.i	0.8985	0.3564

pu-met-fast-016-001.i

pu-met-fast-045-005.i

......

0.8965

0.8954

0.3364

0.3259

Traditional Validation Results: USL = 0.99-MOS-AoA = 0.97 - AoA

## **Example 6**

# 20 kg HEU Billet, Reflected by graphite and Furnace insulation

### Ex 6: HEU Cylinder with Graphite & Furnace Reflection

### **MCNP6** Input

- 20 kg HEU cylinder
- HEU density: 18.95 g/cm<sup>3</sup>
- Graphite density:
   2.25 g/cm<sup>3</sup>
- Furnace insulation density: Al<sub>2</sub>O<sub>3</sub>, 0.5 g/cm<sup>3</sup>
- Reflected with 15 cm graphite, followed by 15 cm insulation

```
billet: g U metal billet
c reflected various thicknesses of graphite,
        2.25 g/cc CRC Handbook 68th Ed
C
 reflected various thicknesses of insulation Al203,
С
          0.5 \text{ g/cc}
С
   V = h*pi*r^2 = h/d*2*pi*r^3
С
  r = (V/(2piH/D)^{(1/3)})
С
 666
       pi
                    = 3.141592654
С
c @@@
                    = 20000
       mass u
                    = 18.95
c 666
       dens u
c @@@
       thick graph = 15
       thick insul = 15
c @@@
c @@@
       vol u
                    = (mass_u/dens_u)
c @@@
       hd
                  = 1.0
c 666
                    = ((vol u / (2*pi*hd))**(1/3))
       r u
       h_u
r_graph
r_insul
c @@@
                    = (2*r \ u*hd)
c @@@
                    = (r u + thick graph)
c 666
                    = (r u + thick graph + thick insul)
c @@@
                    = (h_{u}/2)
       ksrc z
         -1\overline{8}.95 -1
1
     2
                          imp:n=1
10
     1
       -2.25
                 +1 -10
                          imp:n=1
20
     3
       -0.50
                 +10 -20 imp:n=1
                 +20 -30 imp:n=1
30
     0
40
                 +30
                          imp:n=0
     0
 1 rcc 0 0 0 0 0 h u r u
10 rcc 0 0 0
                0 0 h u
                           r graph
20 rcc 0 0 0
                0 0 h u
                           r insul
30 \text{ rcc } 0 0 - 3
                 0 \quad 0 \quad \overline{5}0
                            50
kcode 10000 1.0 100 300
ksrc 0 0 ksrc z
m1 6000.80c
               1.0
mt1 grph.20t
m2 92235.80c -0.93 92238.80c -0.07
m3 8016.80c 0.6
                    13027.80c 0.4
```

•••

### Ex 6: HEU Cylinder with Graphite & Furnace Reflection

calc margin 0.01023	data unc (1-sigma) 0.00104	base USL 0.98	line 208	k(cal) > USL -0.12	<mark>c)</mark> 937
Benchma	rk population	. =	64		
Populat	ion weight	=	26.	06175	
Monimum	aimilarit.	_	201	00052	
Maximum	Similarity	-	0.	90955	
Bias		=	0.	00600	
Bias unce	ertainty	=	0.0	00423	
Nuc Data	uncert margi	n =	0	00104	
Software	/mothod margi	n =	0.0	00104	
Non			0.0	00500	
Non-cove	rage penalty	-	0.0	00000	
bencl	nmark		ck		weigh
heu-met-t	fast-084-004.	i	0.98	95	1,000
heu-met-t	fast-041-003.	i	0.98	95	0.999
heu-met-	fast-084-023.	- i	0.98	78	0.877
heu-met-	fast-019-001.	i	0.98	65	0.780
heu-met-	fast-020-002.	i	0.98	56	0.719
heu-met-	fast-084-001.	i	0.98	50	0.674
heu-met-	fast-084-017.	i	0.98	44	0.631
heu-met-	fast-078-025.	i	0.98	42	0.618
heu-met-	fast-100-001.	i	0.98	41	0.613
heu-met-	fast-041-004.	i	0.98	40	0.606
heu-met-	fast-100-002.	i	0.98	40	0.604
heu-met-	fast-084-015.	i	0.98	37	0.579
heu-met-	fast-089-001.	i	0.98	35	0.563
heu-met-	fast-084-011.	i	0.98	34	0.560
heu-met-	fast-001-001.	i	0.98	32	0.543
heu-met-	fast-022-002.	i	0.98	30	0.532
heu-met-	fast-078-027.	i	0.98	26	0.502
hou_mot_	$f_{act} = 051 - 002$	i	0 98	26	0 499

benchmark	ck	weight
heu-met-fast-078-039.i	0.9825	0.4944
heu-met-fast-078-031.i	0.9825	0.4933
heu-met-fast-078-037.i	0.9824	0.4913
heu-met-fast-012-001.i	0.9824	0.4855
heu-met-fast-078-023.i	0.9823	0.4840
heu-met-fast-084-016.i	0.9823	0.4809
heu-met-fast-084-005.i	0.9823	0.4781
heu-met-fast-078-035.i	0.9821	0.4663
heu-met-fast-084-022.i	0.9821	0.4645
heu-met-fast-044-003.i	0.9818	0.4438
heu-met-fast-044-005.i	0.9818	0.4423
heu-met-fast-018-002.i	0.9815	0.4266
heu-met-fast-044-002.i	0.9814	0.4185
heu-met-fast-051-004.i	0.9814	0.4173
heu-met-fast-044-004.i	0.9814	0.4158
heu-met-fast-063-001.i	0.9811	0.3960
heu-met-fast-010-001.i	0.9810	0.3840
heu-met-fast-044-001.i	0.9808	0.3761
heu-met-fast-078-003.i	0.9808	0.3750
heu-met-fast-007-019.i	0.9807	0.3657
heu-met-fast-010-002.i	0.9806	0.3613
heu-met-fast-008-001.i	0.9806	0.3560
heu-met-fast-084-002.i	0.9804	0.3452
heu-met-fast-063-002.i	0.9803	0.3345
heu-met-fast-084-026.i	0.9802	0.3279
heu-met-fast-079-001.i	0.9801	0.3235
heu-met-fast-065-002.i	0.9796	0.2883
heu-met-fast-041-005.i	0.9796	0.2866
heu-met-fast-079-002.i	0.9794	0.2752
heu-met-fast-043-001.i	0.9794	0.2736
heu-met-fast-084-019.i	0.9794	0.2701
heu-met-fast-084-027.i	0.9793	0.2624

## **Example 7**

# 20 kg HEU Cylinder, Reflected by tantalum

### **MCNP6** Input

- 20 kg HEU cylinder
- HEU density: 18.95 g/cm<sup>3</sup>
- Tantalum density: 16.65 g/cm<sup>3</sup>
- Tantalum reflector thickness: 0 – 15 cm
- Reflected radially

```
billet: g U metal billet, various thick of Ta
reflection
С
 V = h*pi*r^2 = h/d*2*pi*r^3
С
c r = (V/(2piH/D)^{(1/3)})
С
c @@@ pi
                   = 3.141592654
               = 20000
= 10
c @@@ mass u
c @@@ dens u
       thick ta
                   = 0.001, 2, 4, 6, 8, 10, 15
c @@@
c 666
       vol_u
                   = (mass u/dens u)
c @@@ hd
                   = 1.0
c @@@ r_u
c @@@ h_u
                   = ((vol_u /(2*pi*hd))**(1/3))
                   = (2*r u*hd)
      r ta
                   = (r u + thick ta)
c @@@
c @@@
                   = (h_u/2)
       ksrc_z
С
С
     2 - 18.95 - 1
                       imp:n=1
1
10
     1 - 16.65 + 1 - 10
                       imp:n=1
                +10 -30 imp:n=1
30
     0
                +30
                        imp:n=0
40
     0
1 rcc 0 0 0 0 0 h u r u
10 rcc 0 0 0
               0 0 h u
                         r ta
30 \text{ rcc } 0 0 - 3
                0 0 50
                          50
kcode 10000 1.0 100 300
ksrc 0 0 ksrc z
С
m1
    73181.80c
                1.0
С
```

m2 92235.80c -0.93 92238.80c -0.07



No Reflection			benchmark	ck
calc data unc ba	seline k(ca	lc)	heu-met-fast-044-003.i	0.9595
margin (l-sigma) US	L > US	L 4 1 7 2	heu-met-fast-084-015.i	0.9591
0.01803 0.00119 0.9	-0.2	41/3	heu-met-fast-078-041.i	0.9587
Benchmark population	= 57		heu-met-fast-084-017.i	0.9582
Population weight	= 27.93047		heu-met-fast-044-005.i	0.9576
Maximum similarity	= 0.97078		heu-met-fast-084-019.i	0.9576
Maximum Similarity	0.97070		heu-met-fast-043-002.i	0.9575
Rias	= 0.00608		heu-met-fast-044-004.i	0.9572
Rias uncertainty	= 0.00995		heu-met-fast-022-002.i	0.9565
Nuc Data uncert margin	= 0.00000000000000000000000000000000000		heu-met-fast-025-001.i	0.9563
Software/method margin	= 0.00500		heu-met-fast-089-001.i	0.9557
Non-coverage penalty	= 0.00000		heu-met-fast-079-003.i	0.9551
don-coverage penalty	- 0.00000		heu-met-fast-084-022.i	0.9550
benchmark	ck	weight	heu-met-fast-084-004.i	0.9530
neu-met-fast-100-002.i	0.9708	1.0000	heu-met-fast-043-003.i	0.9520
neu-met-fast-100-001.i	0.9707	0.9989	heu-met-fast-027-001.i	0.9518
heu-met-fast-001-001.i	0.9707	0.9978	heu-met-fast-092-001.i	0.9511
heu-met-fast-018-002.i	0.9672	0.8851	heu-met-fast-079-005.i	0.9505
heu-met-fast-065-002.i	0.9665	0.8642	heu-met-fast-084-023.i	0.9505
neu-met-fast-015-001.i	0.9663	0.8577	heu-met-fast-084-012.i	0.9501
neu-met-fast-007-019.i	0.9662	0.8559	heu-met-fast-079-004.i	0.9497
heu-met-fast-051-002.i	0.9657	0.8403	heu-met-fast-084-016.i	0.9493
heu-met-fast-008-001.i	0.9643	0.7960	heu-met-fast-084-002.i	0.9490
neu-met-fast-051-004.i	0.9630	0.7530	heu-met-fast-084-005.i	0.9488
heu-met-fast-044-001.i	0.9628	0.7478	heu-met-fast-020-002.i	0.9483
neu-met-fast-079-001.i	0.9624	0.7355	heu-met-fast-043-004.i	0.9473
neu-met-fast-044-002.i	0.9621	0.7259	heu-met-fast-043-005.i	0.9464
neu-met-fast-007-001.i	0.9620	0.7204	heu-met-fast-087-001.i	0.9461
neu-met-fast-043-001.i	0.9613	0.7013	neu-met-fast-078-023.1	0.9453
neu-met-fast-012-001.i	0.9611	0.6922	heu-met-fast-084-007.1	0.9451
neu-met-fast-084-001.i	0.9602	0.6645	heu-met-fast-063-001.i	0.9441
heu-met-fast-079-002.i	0.9600	0.6580	heu-met-tast-019-001.i	0.9427
			neu-met-iast-041-003.1	0.9426

2cm Tant	alum Reflection	נ			bonchmark	ck	woight
calc	data unc ba	aseline k(ca	lc)	ho	$\frac{\text{Deficiting I K}}{\text{Deficiting I K}}$	0 521 <i>4</i>	
margin	(1-sigma) US	SL > US	L	het	1 - met - 1ast - 044 - 003.1	0.5314 0.5314	0.8928
0.02083	0.00730 0.9	95519 -0.1	5947	her	1 - met - 1ast - 043 - 001.1	0.5314 0.5212	0.0924
			Г	Trouble I	mot fact 070 002 i	0.5312	0.0045
Benchma	rk nonulation	= 118		Ronchmarke	-met-iast-0/9-002.1	0.5310	0.0790
Deneilat	ion unight	- 71 52247		Deficilitat KS		0.5310	0.0775
		- /1.5234/		are not very	-met-last-044-004.1	0.5308	0.0710
Maximum	similarity	= 0.53482	<b>~</b> /	Similar to	-met-iast-089-001.1	0.5307	0.8702
			/L	application		0.5307	0.0091
Bias		= 0.01064	/ -	her	$- met - 1ast - 084 - 004 \cdot 1$	0.5300	0.00/4
Bias unc	ertainty	= 0.01019		net		0.5304	0.8013
Nuc Data	uncert margin	= 0.00730		neu		0.5302	0.8533
Software	/method margin	= 0.00500		net		0.5300	0.0400
Non-cove	rage penalty	= 0.00000		neu		0.5298	0.8424
			<b>V</b>	neu		0.5291	0.8204
hong	hmark	ak	woid	net wht has		0.5290	0.8149
benc	fact 100 002 i	CK 0 5249		net net		0.5288	0.810/
heu-met-	$f_{ast} = 100 - 002.1$	0.5340				0.528/	0.8069
heu-met-	$f_{ast} = 100 - 001.1$	0.5348	0.93			0.5286	0.8043
heu-met-	$f_{ast} = 001 - 001 \cdot 1$	0.5345	0.90		1-met-fast-02/-001.1	0.5284	0./95/
heu-met-	135t - 051 - 002.1	0.5338	0.90	hei	1-met-fast-084-002.1	0.5280	0.7858
heu-met-	1ast-018-002.1	0.5330	0.94	$\frac{1}{2}$ here	1-met-fast-078-023.1	0.5279	0.7828
heu-met-	1ast-00/-019.1	0.5330	0.94	126 hei	1-met-fast-043-003.1	0.5278	0.7787
neu-met-	fast-051-004.1	0.5329	0.94	106 hei	1-met-fast-063-001.1	0.5274	0.7650
neu-met-	Iast-065-002.1	0.5327	0.93	hei	1-met-fast-041-003.1	0.5273	0.7630
neu-met-	fast-015-001.1	0.5326	0.94	284 hei	1-met-fast-079-005.1	0.5273	0.7614
heu-met-	fast-084-001.1	0.5324	0.92	239 hei	1-met-fast-079-004.i	0.5271	0.7571
heu-met-	fast-008-001.1	0.5323	0.92	208 hei	1-met-fast-084-012.i	0.5271	0.7557
heu-met-	fast-044-001.1	0.5321	0.91	147 hei	1-met-fast-019-001.i	0.5269	0.7503
heu-met-	fast-044-002.1	0.5320	0.91	ll5 heu	1-met-fast-087-001.i	0.5267	0.7419
neu-met-	tast-084-017.i	0.5319	0.90	hei hei	1-met-fast-092-001.i	0.5266	0.7391
heu-met-	fast-079-001.i	0.5319	0.90	073 hei	1-met-fast-078-025.i	0.5263	0.7314
heu-met-	fast-084-015.i	0.5317	0.90	024 hei	1-met-fast-043-004.i	0.5259	0.7187
heu-met-	fast-007-001.i	0.5317	0.90				
heu-met-	fast-012-001.i	0.5317	0.90	013			

- None of the benchmarks appear to have the same neutronics as the application
  - Largest C<sub>k</sub> in the Whisper example output is 0.53 – very low
  - Guidance from ORNL
     Scale/Tsunami developers:

$0.95 < C_k$		$\rightarrow$	great
0.90 < C <sub>k</sub>	< 0.95	$\rightarrow$	good
C <sub>k</sub>	< 0.90	$\rightarrow$	not so good

- If all C<sub>k</sub>'s are low, there is a need to expand the benchmark suite, add similar benchmarks
- If no similar benchmarks, need extra analysis, analyst judgment, & margin



- The current benchmark suite for Whisper was focused on main needs for validation, few benchmarks with Ta
- Need to find more benchmarks with Ta reflector & add to Whisper suite, if Ta-reflected applications are expected

## **Example 8**

# Revisiting a Practical Application of the SPSL for Pu Metal

### Example 8: Revisiting a Practical Application of the SPSL for Pu Metal

- LANL undertook an effort to define a threshold between un-moderated and moderated plutonium metal systems in LA-UR-07-0160, *Practical Application* of the Single-Parameter Subcritical Mass Limit for Plutonium.
- The goal was to answer the question of when do plutonium metal and water mixtures cease to appear as "metal" systems and begin to appear more like "solution" systems.
- The study involving plutonium (<sup>239</sup>Pu) metal cubes in water was performed using MCNP. This study is revisited, and Upper Subcritical Limits (USLs) are presented, using WHISPER.



N = 1, Mass Per Cube = 5,000 g, Spacing = N/A



N = 15, Mass Per Cube = ~1.48 g, Spacing = 1 cm

#### Example 8: Revisiting a Practical Application of the SPSL for Pu Metal



### Example 8: Revisiting a Practical Application of the SPSL for Pu Metal



## **Example 9**

## **Pu Critical Mass & USL Curves**

### **Example 9: Critical-Mass and USL-Mass Curves**



### **Example 9: Critical-Mass and USL-Mass Curves**

#### [ANSI/ANS-8.24 7.2]

The validation applicability should not be so large that a subset of data with a high degree of similarity to the system or process would produce an upper subcritical limit that is lower than that determined for the entire set. This criterion is recommended to ensure that a subset of data that is closely related to the system or process is not nonconservatively masked by benchmarks that do not match the system as well.



#### **THERMAL**

- Average neutron energy causing fission: 0.00854 MeV
- % of fissions caused by neutrons: 96%; 3.5%; 0.5%
- Bias+bias uncertainty: 0.01306
- Nuclear data uncertainty: 0.00057
- USL = 0.98046

#### **INTERMEDIATE**

- Average neutron energy causing fission: 0.519 MeV
- % of fissions caused by neutrons: 18%; 55%; 27%
- Bias+bias uncertainty: 0.02197
- Nuclear data uncertainty: 0.00162
- USL = 0.96881

#### <u>FAST</u>

- Average neutron energy causing fission: 1.92 MeV
- % of fissions caused by neutrons: 0%; 2%; 98%
- Bias+bias uncertainty: 0.01419
- Nuclear data uncertainty: 0.00073
- USL = 0.97891

## Using Whisper to Support NCS Validation

## ANSI/ANS-8.24 Requirements & Recommendations

Computer Code System	Whisper-1.1
Verification prior to validation (document)	Developers run verification suites and document results.
	Users must verify installation and operation prior to validation.
Configuration Control	Users must manage configuration.
Changes evaluated to determine	Recommend running MCNP6 validation_criticality V&V suite frequently (daily) to look for changes.
effect on validation	If changes, determine the cause & fix if possible.
	If necessary, complete new sensitivity profiles for Whisper benchmark library.

Selection and Modeling of Benchmarks	Whisper-1.1		
Appropriate process parameters correlate experiment to application	Whisper selects benchmark experiments that are most		
Identify normal and credible abnormal conditions when determining parameters and values (benchmarks should encompass range)	similar to the application using sensitivity profiles to characterize the neutronics of each application and benchmark for each isotope, reaction and energy.		
Use the same methods and analysis to analyze benchmark and application	Whisper uses same methods and analysis for both.		
Review benchmarks prior to use (should be consistent with modeling capabilities of method; drawn from multiple series; evaluated by organization performing validation)	Benchmark models consistent with MCNP6 capabilities; drawn from multiple series; modeled by experienced MCNP6 users; must be reviewed and evaluated by organization performing validation.		
Experienced users responsible for modeling benchmarks			

### **ANS-8.24**

Establishment of Bias, Bias Uncertainty, Margins	Whisper-1.1
Justify positive bias	Does not use positive bias.
Base trending parameters on application	Establishes USL for each application.
Rejection of outliers based on physical behavior or established statistical rejection methods	Rejection based on GLLS with iterative- diagonal $\chi^2$ rejection technique.
Calculational margin consistent with quality and quantity of benchmarks	Selects similar (quality) benchmarks to conduct valid statistical analysis (quantity).
Method consistent with intended use	Consistent (no assumption of normality)
Bias uncertainty allowance for measurement uncertainties; limitations in representations, statistical and convergence uncertainties	Uses experimental and cross-section uncertainties; statistical and convergence uncertainties; parameter studies used for variations in geometry & materials.
Trends used for extrapolation/wide interpolation based on cause	Application-specific USL, possible to trend with output information or parameter study.

### ANS-8.24

Establishment of Bias, Bias Uncertainty, and Margins Margin of Subcriticality (MOS)	
	MOS <sub>data</sub> based on sensitivity profiles and nuclear data covariances,
Sufficiently large to ensure calculated conditions will actually be subcritical	MOS <sub>code</sub> 0.005 based on MCNP developer expert judgment,
	MOS <sub>application</sub> must be applied by NCS analyst.
Take into account sensitivity of application to variations in fissile form, geometry, characteristics. Single trend might not be appropriate over entire validation applicability.	Application-specific, see case study for cubic array of metal pieces.

### ANS-8.24

Adequacy of the Validation			
Validation applicability based on	Sensitivity profiles to select most similar benchmarks, ranked by c <sub>k</sub> .		
benchmark applicability (may be extended)	Non-similar benchmarks (extrapolate or wide interpolate) have lower c <sub>k</sub> ;		
	c <sub>k</sub> < 0.8 requires additional margin based on expert judgment.		
USL based on CM and MOS	USL = 1 - CM - MOS		
The validation applicability should not be so large that a subset of data with a high degree of similarity to the system or process would produce a higher USL than is lower than that determined for the entire set.	Application-specific USL See Whisper Case Study Critical Mass		
Subset of data closely related to application is not nonconservatively masked by benchmarks that do not match the system as well.	Curve		

- Documentation and Independent Technical Review
  - Trending analysis and technical basis
  - Validation applicability
  - Differences validation applicability application
  - Limitations
  - MOS and its basis
  - USL and methods to determine
  - Independent technical review
    - Benchmark applicability
    - Input/output files
    - Methodology: CM, MOS
    - Concurrence with validation applicability

# References

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All references are available at URL: mcnp.lanl.gov  $\rightarrow$  Recent Publications  $\rightarrow$  Whisper – NCS Validation

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